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# Separation efficiency and ice strength properties in simulated natural freezing of aqueous solutions

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## Abstract

In geographical regions with sub-zero temperatures, natural freezing can potentially be used as an energy-efficient purification technique for industrial wastewaters. The utilization of this technique requires knowledge of the effect of impurities on the strength of the ice to enable the effective harvesting of produced ice. Previous studies of the mechanical properties of model-scale ice have tended to focus on the initial solution, and little consideration has been given to the amount of impurities trapped inside the ice. The aim of this research is to evaluate the separation efficiency during the natural freezing process by quantifying the impurities trapped inside the ice formed from known concentrations of aqueous solutions and to investigate the effect of impurities on the bulk mechanical properties of the ice.

In this study, twenty similar size ice beams were prepared in freezing boxes in a temperature-controlled cold room from five different aqueous solutions – tap water, and ethanol and sodium chloride aqueous solutions of two different molalities, i.e. 0.1 mol/kg and 0.3 mol/kg. The

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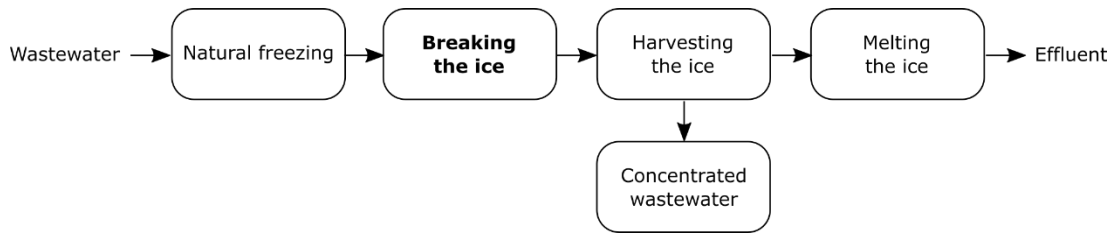
27 bending strength and natural frequencies of the ice samples were measured in the freezing  
28 conditions, and the concentrations of impurities in melted ice samples were determined. The  
29 research shows that with the ethanol and sodium chloride solutions, the concentration of  
30 impurities inside the ice clearly decreased in comparison to the initial solution. The structure  
31 of the ice from the different solutions differed significantly; as the tap water formed columnar  
32 ice, ethanol ice grew through large platelets, while the structure of the sodium chloride ice was  
33 a mixture of the two forms. The tap water yielded the highest strength ice and the ice formed  
34 from the ethanol aqueous solutions the weakest ice. The measurements indicated that the  
35 concentration of impurity in the ice reduces the mechanical strength and the magnitude of the  
36 effect varies with the chemical characteristic of impurity.

37 Keywords: Flexural strength; Ice purity; Natural freezing; Natural frequency

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## 38 **1 Natural freeze crystallization and mechanical properties of ice**

39 The insufficiency of accessible water and worsening of water quality due to industrial  
40 discharges have made it necessary to find alternative and energy efficient water purification  
41 methods. The conventional processes to treat wastewaters are adsorption, chemical  
42 precipitation, electrolytic treatment, flotation, ion exchange, and membrane filtration, which all  
43 have unique properties and suitable water types. Natural freezing is an alternative method to  
44 achieve purification. When freezing is implemented in a wastewater basin under natural  
45 weather conditions, the cooling energy of arctic sub-zero temperature regions can be utilized  
46 to energy efficient wastewater treatment. A pure ice layer is forming over the wastewater basin  
47 similar way as in lakes, rivers and seas. A conceptual approach for wastewater purification by  
48 natural freezing is presented in Fig. 1.



49

50 **Fig. 1** Conceptual approach for wastewater purification by natural freezing.

51 During the freezing of a solution, heat of crystallization is released into the surroundings. The  
 52 ice crystal lattice usually rejects solute molecules/ions because of their excessive size,  
 53 preventing the formation of a solid solution with water (Petrich and Eicken, 2010). Thus,  
 54 solutes redistribute during ice crystallization. The extent of the redistribution is attributed to the  
 55 capability of the solute to diffuse away from the ice-solution interface (Butler, 2002).  
 56 Succeeding these points of view, the temperature and concentration gradients are created  
 57 adjacent to the growing ice front (Butler, 2002; Hasan and Louhi-Kultanen, 2015). Sea ice is  
 58 a paradigm of natural freezing. The main source of impurity in sea-ice is the formation of brine  
 59 pockets within the ice matrix (García et al., 2014). Analogously, the impurity of ice forming  
 60 from any type of solution could be interpreted by the entrapment of the freeze concentrated  
 61 solution in the ice crystal lattice. The efficiency of natural freezing is influenced by solution  
 62 concentration and different growth conditions, such as the ambient temperature, freezing time  
 63 and freezing rate. The effect of these factors on ice purity is epitomized by ice formation from  
 64 sodium sulphate solutions. Experimental results show that a lower growth rate and solution  
 65 concentration are in favour of higher ice purity (Butler, 2002).

66 The mechanical properties of ice have been the interest of research in glaciology and  
 67 geosciences for decades (Schulson and Duval, 2009) and many different methods have been  
 68 utilized in various studies. The dynamic modulus of elasticity of freshwater and saline ice has  
 69 been studied by Snyder et al. (2016) with ultrasonic measurement. The effect of porosity on

70 the dynamic modulus of elasticity found to be aligned with earlier researches (Snyder et al.,  
71 2015; Schulson and Duval, 2009). Yasui et al. (2017) used a three-point bending test for  
72 determining the fracture toughness of ice. The Acoustic Emission (AE) was utilized to detect  
73 failure in a cyclic test of ice (Hammond et al., 2018). The effects of various mixtures of  
74 compounds on formed ice have also been an interest of studies. Recent research has been  
75 focused on studying the effect of freshwater ice and silica mixture on the mechanical properties  
76 of ice (Yasui et al., 2017) and sulfuric acid doped ice under tension and compression  
77 (Hammonds and Baker, 2018). The effects of Ca<sup>++</sup> doped ice to the ice strength (Hammonds  
78 and Baker, 2016) and the mechanical properties of saline ice (Snyder et al., 2016) have been  
79 studied as well.

80 The strength of sea ice and parameters affecting the strength have been the object of study  
81 for decades. In terms of impurities, the salinity (through brine volume) has been observed to  
82 have a clear effect on the mechanical properties of ice, see e.g. Timco and O'Brian (1994) for  
83 the flexural strength and Timco and Weeks (2010) for modulus of elasticity. Timco and O'Brien  
84 (1994) have combined several databases and shown that the flexural strength can be  
85 determined based on the square root of the brine volume, which can be determined based on  
86 temperature and salinity. Values over 1.5 MPa have been measured for the flexural strength  
87 of first-year sea ice, but values typically range from 1 MPa and decrease with the brine volume,  
88 being of the order of 100 to 150 kPa for warm sea ice (Timco and Weeks, 2010). The estimates  
89 for the flexural strength of old ice, i.e. second year and multiyear sea ice, would be of the order  
90 of 0.8 to 1.1 MPa in the winter and 0.4 to 0.6 MPa in the summer (Timco and Weeks, 2010).  
91 In the Baltic Sea, the four-point bending tests have shown the flexural strength to be 0.58 MPa  
92 on average and from 0.42 MPa to 0.55 MPa when determined from cantilever beam tests  
93 (Enkvist, 1972; Määttänen, 1976; Kujala et al., 1990).

94

95 In addition, the studies have shown that the brine volume has a clear effect on the elastic and  
96 static modulus. The elastic modulus here refers to Young's modulus ( $E$ ) determined with  
97 dynamic measurements and a static modulus to Young's modulus determined from static  
98 tests. The dynamic measurements are commonly determined by measuring the rate of wave  
99 propagation in ice or by exciting the natural resonant frequencies of different vibration modes  
100 (Weeks and Hibler, 2014). The experimental results have shown that the values of the elastic  
101 modulus vary between 1.7 and 5.7 GPa when determined from flexural waves, and from 1.7  
102 to 9.1 GPa when determined from body-wave velocities (Weeks and Assur, 1968). Anderson  
103 (1958) has shown that there is a clear decreasing trend in the elastic modulus as a function of  
104 brine volume. The static modulus for sea ice has been commonly determined from the bending  
105 tests (see e.g. Dykins, 1971). Similar to dynamic tests, the static tests have shown that the  
106 static modulus decreases as a function of brine volume (see e.g. Vaudrey, 1977). The static  
107 modulus measurements have shown a great scatter and the values have been, on average,  
108 between 1 and 5 GPa (Timco and Weeks, 2010). For more detailed discussions on the effect  
109 of brine volume and other environmental factors on the elastic and static modulus of sea ice,  
110 see (Borland, 1988; Hirayama, 1983; Lau et al., 2007; Lehmus, 1988; Nortala-Hoikkanen,  
111 1990; Riska et al., 1994; Weeks and Hibler, 2014).

112

113 Besides salt (sodium chloride), the development of model scale ice has raised interest towards  
114 the effect of other chemicals on the strength of ice. The general conclusion is that adding these  
115 dopants to the water weakens the formed ice in terms of flexural strength (e.g. Borland, 1988),  
116 and the elastic modulus (Hirayama, 1983). As the flexural strength has been considered the  
117 most important mechanical property of ice for ship model scale testing, the development has  
118 focused on scaling the flexural strength correctly and then confirming that the ratios between

119 other parameters are in the same range as with sea ice. Due to the typical size of the ships  
120 with respect to the size of the model scaled ships, the typical scale ratio for the model is 10 to  
121 40, and thus, the required flexural strength is from 15 kPa to 60 kPa in model scale (Lau et al.,  
122 2007). Therefore, the minimum for the ratio between the static modulus and the flexural  
123 strength is 2000, and it can reach a value of 8000 (see e.g. Riska et al., 1994; Timco, 1980).

124

125 Timco (1981) conducted the most extensive flexural strength tests with different chemicals.  
126 The chemicals included acetates, amides, various inorganic salts as well as sucrose with fixed  
127 mass fractions (Timco, 1981). Timco (1981) compared the influence of various mass fractions  
128 of the selected chemicals on the flexural strength of ice. The higher mass fractions led to lower  
129 flexural strength of ice (Timco, 1981). Furthermore, different model scale basins have ended  
130 up using different chemicals, which include urea, a mixture of ethylene glycol, aliphatic  
131 detergent and sugar (EG/AD/S), alcohol and sodium chloride (see e.g. Borland, 1988;  
132 Hirayama, 1983; Lau et al., 2007; Riska et al., 1994; Lehmus, 1988; Nortala-Hoikkanen, 1990),  
133 for studies with different types of model scale ice. The measurements have shown that with  
134 these chemicals combined with different ice production methods (seeding or spraying) the  
135 flexural strength can be scaled to 15-60 kPa with different solutions (Lau et al., 2007).  
136 However, the measurements have shown that the ratio between the elastic modulus and the  
137 flexural strength of the urea doped model ice is  $\leq 2000$  (Hirayama, 1983; Narita et al., 1988).  
138 The range for EG/AD/S doped ice is 1000–3000 (Timco, 1986) and for the correct density  
139 (CD)-EG/AD/S 2000–3250 (Lau et al., 2007). The fine-grained ethanol ice, however, covers  
140 the ratio range of 1750–5000 (Riska et al., 1994).

141

142 However, in the development of the model scale ice, the interest is commonly in the initial

143 solution and freezing process. Thus, the studies generally account for the mass concentration  
144 of the chemical in the initial solution and neglect how much of the chemical is trapped inside  
145 the ice, i.e. the amount of chemical actually affecting the properties of the ice. These  
146 simplifications are usually for practical reasons (it is easier to observe and control the mass  
147 concentration of the initial solution and then check the obtained mechanical properties).  
148 Furthermore, due to the weakening effect of chemicals, the model scale ice is difficult to move  
149 from in-situ without damaging it. Thus, the static modulus is commonly determined from the  
150 plate deflection and the flexural strength is determined from a cantilever beam test, as  
151 recommended by ITTC guidelines (ITTC guidelines, 2014). In addition, the dynamic  
152 measurements are conducted with a scanning laser Doppler vibrometer (SLDV) to measure  
153 the natural frequencies (Polytec, 2017).

154

155 The natural frequencies of the ice indicate the internal structure dynamic behaviour for a  
156 known geometry, i.e. an ice beam. They can be considered a measure determining the  
157 mechanical dynamic property of the ice. (Rao, 2007). The formed ice beams consisted of many  
158 interconnected different shaped, sized and oriented ice crystals. In this study, the complete  
159 ice beam dynamics response was measured. The ice in solid form was then assumed to  
160 behave like a solid particle, where the natural frequencies of a solid particle are fundamentally  
161 related to the square root of mass divided by stiffness (Carvill, 1994). Knowing the natural  
162 frequencies of an ice sample allows calculating the equivalent modulus of elasticity, i.e. the  
163 overall stiffness, which is important to know when modelling the sample that has the same  
164 dynamical behaviour as the actual formed ice. Calculating the modulus of elasticity requires,  
165 in addition, knowledge of the ice sample's physical dimensions, density and area moment of  
166 inertia. For a beam shaped ice piece, the modulus of elasticity can be analytically calculated.  
167 The assumption is that the impurities captured in the ice have an impact on the stiffness of the



168 ice and thus the impurities could be detected from the natural frequencies. The ice can be  
169 excited at natural frequencies, which causes energy to collect in the ice and the ice to yield  
170 and break into smaller parts.

171 In the application of wastewater purification by freezing, measuring and determining the  
172 mechanical properties of ice are important. This information can be used to estimate the ice  
173 strength and to evaluate the needed force for breaking and collecting the ice in a purification  
174 process application. Analysing the ice strength by the four point bending test has been found  
175 to be accurate and commonly used method (Kujala et al., 1990). Compared with the three  
176 point bending test, the shear force does not change rapidly in the location where the failure is  
177 assumed to occur, i.e. in the middle of the loaded beam, as can be seen from beam theories,  
178 see e.g. (Parnes, 2001). The advantage of using simple beam tests over the cantilever beam  
179 tests is that root stresses do not disturb the measurements by lowering the measured flexural  
180 strength values as noted by Timco and O'Brian (1994). The information about the ice  
181 mechanical rigidity can be gained through measuring the natural frequencies. Natural  
182 frequencies can be measured without breaking the ice sample e.g. by exciting the ice  
183 externally, recording the velocity response and post-processing it. Natural frequencies can be  
184 detected with non-contact and non-destructive method, which is beneficial for detecting the  
185 ice mechanical rigidity.

186 Hence, the aim of this research is to determine the amount of ethanol and sodium chloride  
187 trapped inside the laboratory-produced ice and their effect on the mechanical properties of the  
188 ice: the flexural strength, static and dynamic elastic modules. These parameters are required  
189 when designing a wastewater purification apparatus and testing the performance of ice  
190 breaking vessels.

## 191 2 Freezing test procedure

192 To our best understanding, the chemical quantity in the solution determined by the molality  
193 (moles of chemical per kg of water) is a better measure for the comparison of chemical impacts  
194 than using the mass percent (wt-%) based quantity due to the different molar masses of the  
195 studied chemicals. The molar mass of sodium chloride NaCl, 58.443 g/mol, is much higher  
196 than the molar mass of ethanol C<sub>2</sub>H<sub>5</sub>OH, 46.068 g/mol (Haynes, 2017). Due to this fact, in the  
197 present work we fixed the solute quantities based on molality (mol chemical/kg tap water). In  
198 this study, five different solutions were prepared: tap water (basic liquid), two organic aqueous  
199 solutions and two inorganic aqueous solutions, both with two different molal concentrations,  
200 0.1 mol/kg and 0.3 mol/kg. The initial solution was mixed in a 100 kg batch. The solutions were  
201 prepared in room temperature and an agitator was used to achieve sufficient mixing during  
202 dissolution. The initial aqueous ethanol solutions were prepared by dissolving ethanol (ETAX  
203 B16 with 92.4% ethanol content supplied by Altia Industrial) in tap water. The initial aqueous  
204 sodium chloride solutions were prepared by dissolving 99.9% pure sodium chloride (supplied  
205 by VWR Chemicals) in tap water. The tap water was high-quality drinking water with a  
206 temperature of 13 - 15 °C at that time. The quality of water is guaranteed by the water supplier  
207 and contains very low concentrations of impurities due to requirements. Samples of 500 ml  
208 from every five initial solutions were obtained after preparation. The solutions were carried in  
209 lidded containers to a cool storage where they awaited further test preparation.

210

211 After the solutions were prepared, each batch was divided into four freezing boxes made of  
212 insulated material, Finnfoam (housing insulation material, polystyrene), to prevent freezing on  
213 the sides and bottom, i.e. the cold was affecting the surface layer while the foam walls  
214 insulated the sides and bottom, thus replicating natural freezing. Therefore, the heat flux

215 migrated mainly from the solution through the ice layer to cooling air. In total, twenty similar  
216 freezing boxes were used in the freezing experiments. The boxes consisted of outer and inner  
217 boxes. The utilization of two boxes allowed removing of the ice sample with low effort, as the  
218 ice could be taken out easily by lifting the inner box with the sample. The inner dimensions of  
219 the inner boxes were 60 cm in length and 15 cm in width. The depth of the inner box was lower  
220 than the depth of the outer box, as the aim was to freeze half of the solution in maximum.  
221 Thus, the separation efficiency of natural freezing could be kept at moderate level when less  
222 than 50% of solution is frozen (Hasan and Louhi-Kultanen, 2016).

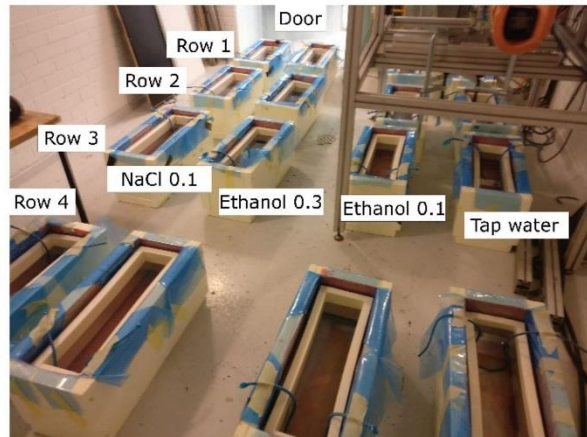
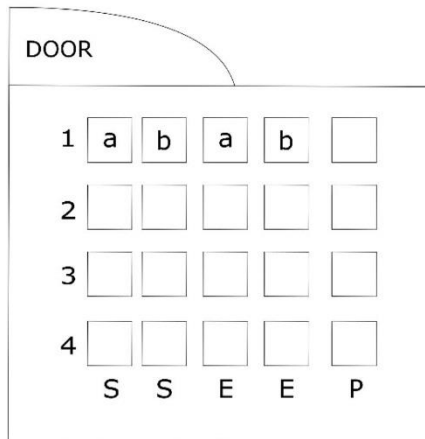
223

224 The interior of the outer freezing box was lined with plastic to make the box waterproof. The  
225 open section between the inner and outer boxes was insulated by placing a piece of joint  
226 insulation foam, commonly used in buildings, between the boxes. Thus, it prevented the boxes  
227 from freezing together. An elastic rope was placed into the box to mount the frozen samples  
228 for the natural frequency measurements. Prior to pouring the solutions, each box was weighed  
229 with a Sartorius LC 34000P balance (capacity 34 kg and readability 0.5 g). Each sample  
230 contained 24 kg of the initial solution and was weighed in room temperature.

231

232 After all of the boxes were prepared, weighed and filled with solutions, the boxes were taken  
233 into the cold room, where the targeted temperature was -5 °C. The samples were placed in  
234 the room in a four by five matrix form where each column formed a line of similar initial  
235 samples. The first row of solutions was closest to the door and the fourth row closest to the  
236 back wall. Fig. 2a shows the arrangement and naming of the samples. The naming is in  
237 sequential order. The first letter "P" refers to the tap water, "E" to the ethanol solution and "S"  
238 to the sodium chloride solution. The preceding numbers 1, 2, 3 and 4 represent the row  
239 number. The third item refers to the molality: "a" to 0.1 mol/kg and "b" to 0.3 mol/kg. The fourth

240 letter refers to the ice section: “t” to the top (upper) section of the ice, “c” the centre section  
 241 and “b” the bottom section. In the results, the naming labels, e.g. “E1at” refers to ethanol  
 242 solution, row 1, molality of 0.1 mol/kg and top section. Fig. 2b shows the freezing arrangement  
 243 in the cold room.



244 a)

b)

245 **Fig. 2** Freezing arrangement. a) Layout of freezing boxes. b) Picture taken in the cold room (NaCl 0.3 has not been  
 246 carried in yet).

247 A temperature sensor was placed in each box in the first row to monitor the temperature in the  
 248 liquid during freezing, and in addition, the ambient temperature was measured from the middle  
 249 of the first row. A total of six PT100 thermometers were connected to two PicoLog PT-104  
 250 data loggers, which were connected via USBs to a laptop.

## 251 2.1 Natural frequency

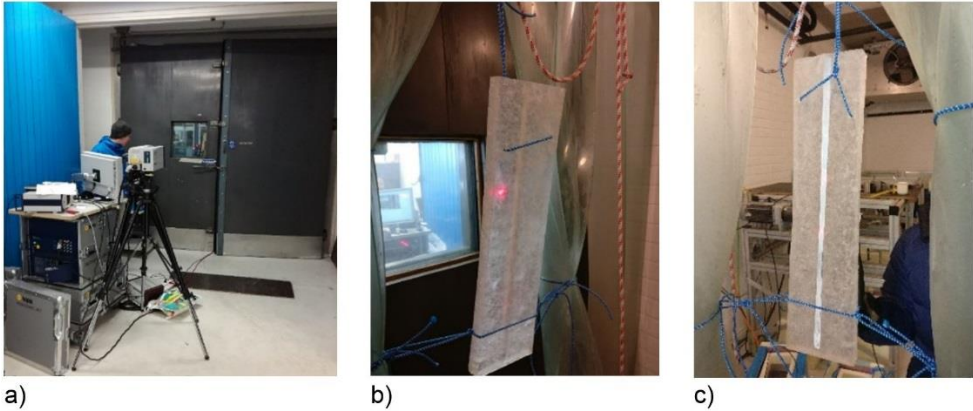
252 The natural frequencies were measured in the cold room to avoid the melting of the ice  
 253 samples. The measurement was conducted with an optical scanning laser Doppler vibrometer  
 254 (SLDV). The SLDV is a non-contact and non-destructive method of measuring surface  
 255 velocities and consequently natural frequencies. The optical signal allows measuring through  
 256 transparent media, e.g. glass or water. It is based on the Doppler effect and measures the

257 surface velocity of excited ice. (Polytec, 2017). In practice, the laser signal is focused on a  
258 predefined plane, which is the front of the measured sample. An example of using SLDV for  
259 measuring through a glass window into a water tank to measure an ultrasonic transducer far-  
260 field characteristics can be seen from Cooling et al. (2010). The ice was excited with a piezo  
261 exciter (PI P-844.10) and the frequency response was recorded at given locations. To be able  
262 to record the reflective laser signal, a 10 mm wide retroreflective tape (A-RET-T010) was  
263 attached by freezing with a small amount of 0 °C tap water vertically on the upper surface of  
264 the ice. The possible detrimental effect of the retroreflective tape on the dynamic motion of the  
265 measurements can be neglected as the thickness of the tape (0.1 mm) is very small in  
266 comparison with the ice thickness (minimum ~30 mm). In addition, the small amount of water  
267 to bond the tape on the ice is so thin that the effect on dynamics is negligible.

268

269 The ice was hung with elastic rope, which was placed in the solution prior to freezing. There  
270 is a large difference in the stiffness of the ice and the elastic rope with which it is hung. This  
271 enables capturing only the ice internal dynamical behavior. The ice samples were also  
272 supported from the bottom to limit the rigid body motion. Fig. 3a depicts the hardware located  
273 outside the cold room: a Polytec PSV-500 scanning head and an OFV-505 reference laser  
274 pointed directly at the glass window. Fig. 3b depicts the ice hanging setup inside the cold room.  
275 The measurement procedure has three initial steps. The first is to set a measurement plane,  
276 that is in this case the top surface of the ice beam. Secondly, the visible laser is focused on  
277 the top of the plane. Thirdly, the 3D orientation is defined by the origo, Y-direction and XY-  
278 plane. The scanning hardware operation temperature is limited to the range of +5 to +40 °C;  
279 thus, the measurement was conducted through the transparent glasses. The piezo exciter's  
280 operating temperature is limited to -20 to +80 °C, and it could thus be used in the cold room to  
281 excite the ice sample. The exciter is made from steel and was stored in the cold room to avoid

282 melting the ice sample when in contact with it. Fig. 3c depicts the front surface of the ice  
 283 sample. The ice pieces that were strong enough to hang from the flexural rope were measured.  
 284 The natural frequencies were measured from the upper surface of the ice and the excitation  
 285 was given from the bottom layer.



287 **Fig. 3** Setup for measuring natural frequencies of the ice samples: a) Polytec vibrometer unit outside of the cold  
 288 room b) ice sample hanging with flexible ropes and stabilized in the bottom with additional flexible ropes. c)  
 289 Retroreflective tape frozen to the front surface of the ice.

290  
 291 The modulus of elasticity (via dynamic measurement)  $E_d$  is calculated based on beam theory

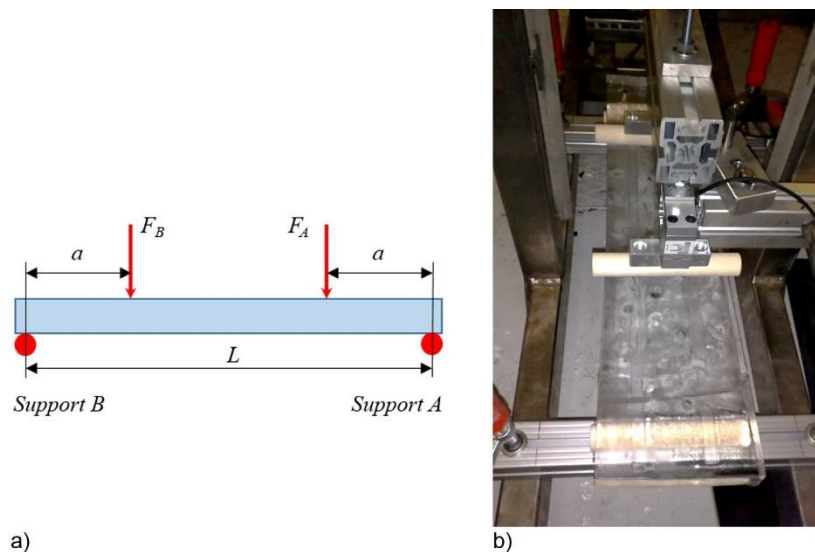
$$E_d = \frac{(f_n \cdot 2\pi)^2 \cdot A \cdot \rho \cdot L_B^4}{k^4 \cdot I}, \quad (1)$$

292 where  $f_n$  is the natural frequency,  $A$  is the cross sectional area,  $\rho$  is the ice density,  $L_B$  is the  
 293 ice beam length,  $k$  is a factor dependent on the support. For free-free supported body, *i.e.*  
 294 freely floating body, as is in this case, the factor for the first flexural natural frequency is 4.730,  
 295 and  $I$  is the area moment of inertia. (Rao, 2007).

## 296 2.2 Flexural strength

297 The flexural strength of ice was measured with a four-point bending test in the cold room. Fig.  
 298 4 presents the test setup. The test sample was placed on top of the rounded wooden supports.

299 The two load sensors were mounted with an aluminium profile onto the electrically driven  
 300 piston. The load sensors were HBM S2M 500N. Rounded wooden parts were attached under  
 301 the sensors, which were in contact with the ice beam in the loading. The rounded wood pieces  
 302 allow rotational movement in the ice under loading. In each test, the displacement was  
 303 measured at the mid span of the ice beam with HBM WA 10 mm displacement sensors. The  
 304 forces and displacement were recorded with a frequency of 1.2 kHz.



306 **Fig. 4** Four-point bending test setup. a) The principle picture from the test. b) The device measuring the P4 ice sample.

307 After the loading, the distance of the breaking point was measured from the left-hand side  
 308 support. In addition, the thickness and the width of the ice beam at the breaking point were  
 309 measured. The ice beam is assumed to behave as an Euler-Bernoulli beam. At first, the  
 310 moment equation along the beam is determined from the free-body diagram. It is assumed  
 311 that the first failure in a bending situation occurs on the surface in tension, as the axial stress  
 312 (in the longitudinal direction) maximum occurs on the surface of the beam. Knowing the  
 313 relation (Parnes, 2001):

$$\sigma_x = \frac{My}{I} \quad (2)$$

314 where  $\sigma_x$  is the axial stress,  $M$  is the moment affecting the cross-section,  $y$  is  
 315 the distance from the neutral axis, and  $I$  is the second moment of inertia.  
 316 Inserting the moment equation in this equation we obtain the following form for  
 317 the flexural strength ( $\sigma_f$ ):

$$\sigma_f = 3 \cdot \frac{(L-x) \cdot x \cdot \rho \cdot g}{h} + 6 \frac{(L-x) \cdot a \cdot F_B + a \cdot x \cdot F_A}{L \cdot b \cdot h^2}, \quad (3)$$

318 where  $L$  is the distance between the supports,  $x$  is the distance of the crack from the left-hand  
 319 side support,  $g$  is the gravitational acceleration,  $h$  is the thickness of ice,  $a$  is the distance of  
 320 a sensor from the same side support,  $F_A$  is the load measured with the right load sensor,  $F_B$   
 321 is the load measured with the left load sensor,  $b$  is the width of the sample.

### 322 2.3 Static modulus of elasticity

323 The displacement was measured simultaneously with the force. This enables the  
 324 determination of the static modulus of elasticity ( $E_s$ ), i.e. the effective Young's modulus. In this  
 325 case, the ice beam is assumed to behave as an Euler-Bernoulli beam. After the moment  
 326 equation along the beam is determined, the displacement equation,  $w$ , for the beam can be  
 327 derived from the following relation (Parnes, 2001):

$$EI \frac{d^2w}{dx^2} = -M(x). \quad (4)$$

328 After the displacement equation is determined and the displacement is measured from a



329 known location, the static modulus ( $E_s$ ) of elasticity can be determined from the following  
 330 equation:

$$E_s = \frac{(34 \cdot a \cdot L^2 - 64 \cdot a^3) \cdot F_B + 16 \cdot a \cdot L^2 \cdot F_A}{384 \cdot I \cdot w_{centre}}, \quad (5)$$

331 where the second moment of inertia ( $I$ ) was determined by measuring the width and the height  
 332 of the tested beam from the location the failure occurred and  $w_{centre}$  is the width at the failure  
 333 location. This assumes the beam is solid with negligible porosity and uniform thickness and  
 334 the width of the beam over the length.

335 Unfortunately, some of the ice beams were broken when taken out from the freezing boxes. 4  
 336 of 30 beams (or halves) broke before the measurements. The fourth row of ice was mainly too  
 337 weak for the bending strength test. Row 2 ice was measured as full beams. Rows 1 and 3 ice  
 338 beams were cut in half for the bending test and static modulus of elasticity. Due to the test set-  
 339 up, it was not possible to mount the displacement sensor on the rig for samples broken when  
 340 taken out from the freezing boxes, as the span between the supports was small.

## 341 2.4 Chemical analyses

342 The formed ice layer and concentrated residual solution under the ice layer were separated  
 343 after the freezing test period by lifting up the ice layer from the freezing box. The total mass of  
 344 the ice layer was weighed and the ice was moved to mechanical testing. A 500 ml sample was  
 345 taken (after agitating the liquid) from the concentrated solution remaining in the box. After the  
 346 mechanical tests of ice (the frequency measurement and flexural strength test), the ice  
 347 samples for chemical analysis were collected within various horizontal layers sliced in sections  
 348 of 1 to 4 cm thicknesses using a band saw. The ice pieces were rinsed with purified water,  
 349 produced by Elga PureLab water system (resistivity 18.2 M $\Omega$ ·cm, TOC < 5 ppb) to avoid

350 external contamination during the ice handling. Composite ice samples from a layer were  
351 collected into a plastic bag for crushing with a hammer. The crushed ice was packed tightly in  
352 250–500 ml polyethylene bottles for freeze storing, transporting and further chemical analysis.  
353 The total amount of samples was 70: 5 initial solution samples, 20 concentrated solution  
354 samples, 10 whole ice layer section cut samples and 35 ice layer samples from different  
355 horizontal layers. Furthermore, vertical and horizontal ice layer samples were cut and collected  
356 from the ice samples in rows two and three to visually observe the crystal structure by placing  
357 the samples between two polarizing films and directing light through the arrangement.

358

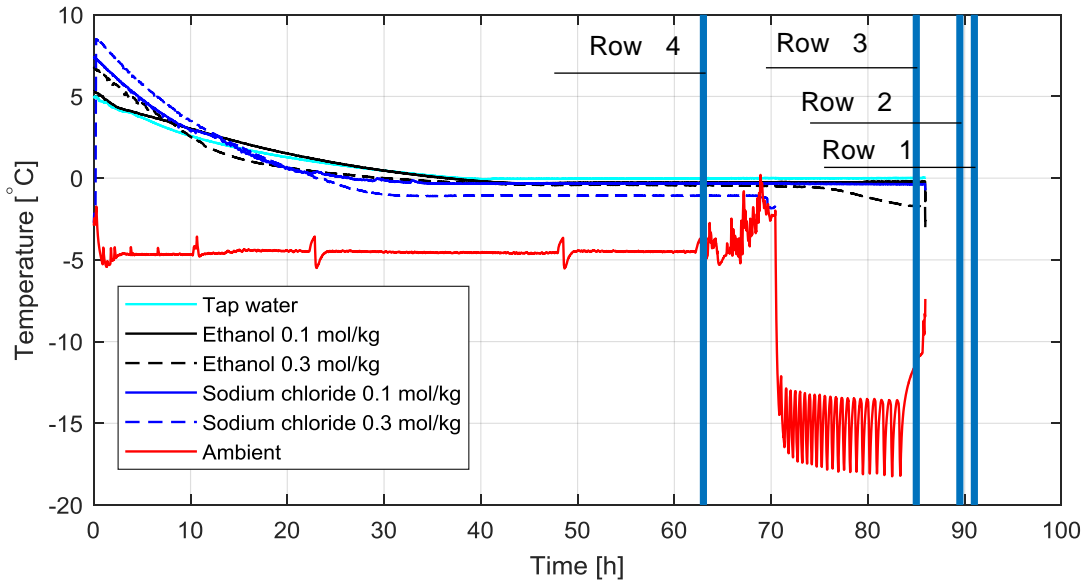
359 All freeze stored samples were melted at room temperature. The samples containing tap water  
360 and ethanol were analyzed with a total organic carbon (TOC) analyser (Shimadzu TOC-L +  
361 ASI-L Autosampler, detection limit 4 µg/l) to determine the concentration of total organic  
362 carbon. Ethanol concentrations were further calculated based on TOC concentrations. Molar  
363 mass of ethanol C<sub>2</sub>H<sub>5</sub>OH is 46.068 g/mol, of which 52.50% is carbon (Haynes, 2017). Electrical  
364 conductivities of samples containing tap water and sodium chloride were measured by a  
365 Consort C3040 Multi-parameter analyser with conductivity electrode SK20T (range 1.0 µS/cm  
366 to 100 mS/cm, cell constant 1.0 1/cm). Sodium chloride concentrations were determined by  
367 linear fitting based on conductivity values reported in literature (Haynes, 2017). The densities  
368 of all samples (melted ice, initial solution and concentrated solution) were determined by an  
369 Anton Paar DMA4500 density meter (repeatability with density  $1 \cdot 10^{-5}$  g/cm<sup>3</sup> and temperature  
370 0.01 °C). NaCl and ethanol concentrations were determined by linear fitting based on density  
371 values reported in literature (Haynes, 2017).

## 372 3 Results

### 373 3.1 Temperature profile

374 The temperatures were recorded from the first row samples with an interval of one minute until  
375 the samples in the second last row (row 2) were taken out from the freezing boxes. Fig. 5  
376 depicts the logged temperature profile, and the vertical lines indicate the times of ice removal  
377 from the boxes. At first, the cooling rates varied considerably due to the diverse temperatures  
378 of the liquids when the cooling and freezing started. After 45 h of freezing, temperatures of  
379 liquids attained final constant temperatures. Tap water, the 0.1 mol/kg NaCl solution and the  
380 0.3 mol/kg NaCl solution stayed at temperatures  $-0.03\text{ }^{\circ}\text{C}$ ,  $-0.33\text{ }^{\circ}\text{C}$  and  $-1.07\text{ }^{\circ}\text{C}$ , respectively,  
381 and were close to known freezing point depression (FPD) temperatures  $\sim 0\text{ }^{\circ}\text{C}$ ,  $-0.34\text{ }^{\circ}\text{C}$  and -  
382  $1.02\text{ }^{\circ}\text{C}$  reported in literature (Haynes, 2017). The ethanol 0.1 mol/kg solution appeared slightly  
383 undercooled with a temperature of  $-0.28\text{ }^{\circ}\text{C}$  when the FPD temperature is  $-0.17\text{ }^{\circ}\text{C}$  (Haynes,  
384 2017). The 0.3 mol/kg ethanol solution was rather warm with a temperature of  $-0.42\text{ }^{\circ}\text{C}$  when  
385 compared to the FPD temperature of  $-0.54\text{ }^{\circ}\text{C}$  (Haynes, 2017). Unexpectedly, this  
386 concentrated ethanol solution also started to cool down after 70 h of freezing, when the  
387 temperature of the freezing room was decreased and the solution reached an undercooled  
388 temperature of  $-1.7\text{ }^{\circ}\text{C}$ . The temperature probe used for the 0.3 mol/kg sodium chloride  
389 solution shows a colder temperature after 70 h, as it was accidentally pulled out from the  
390 solution and exposed to the cold room temperature. The aim was to seed the solutions prior  
391 to ice forming. However, after ten hours, it was noted that frazil natural ice formed on the  
392 surface of tap water and 0.1 mol/kg ethanol solutions as well as rows three and four of 0.3  
393 mol/kg ethanol solutions. Thus, these samples were not seeded, whereas all the sodium  
394 chloride solutions and ethanol solutions E1b and E2b were.

395



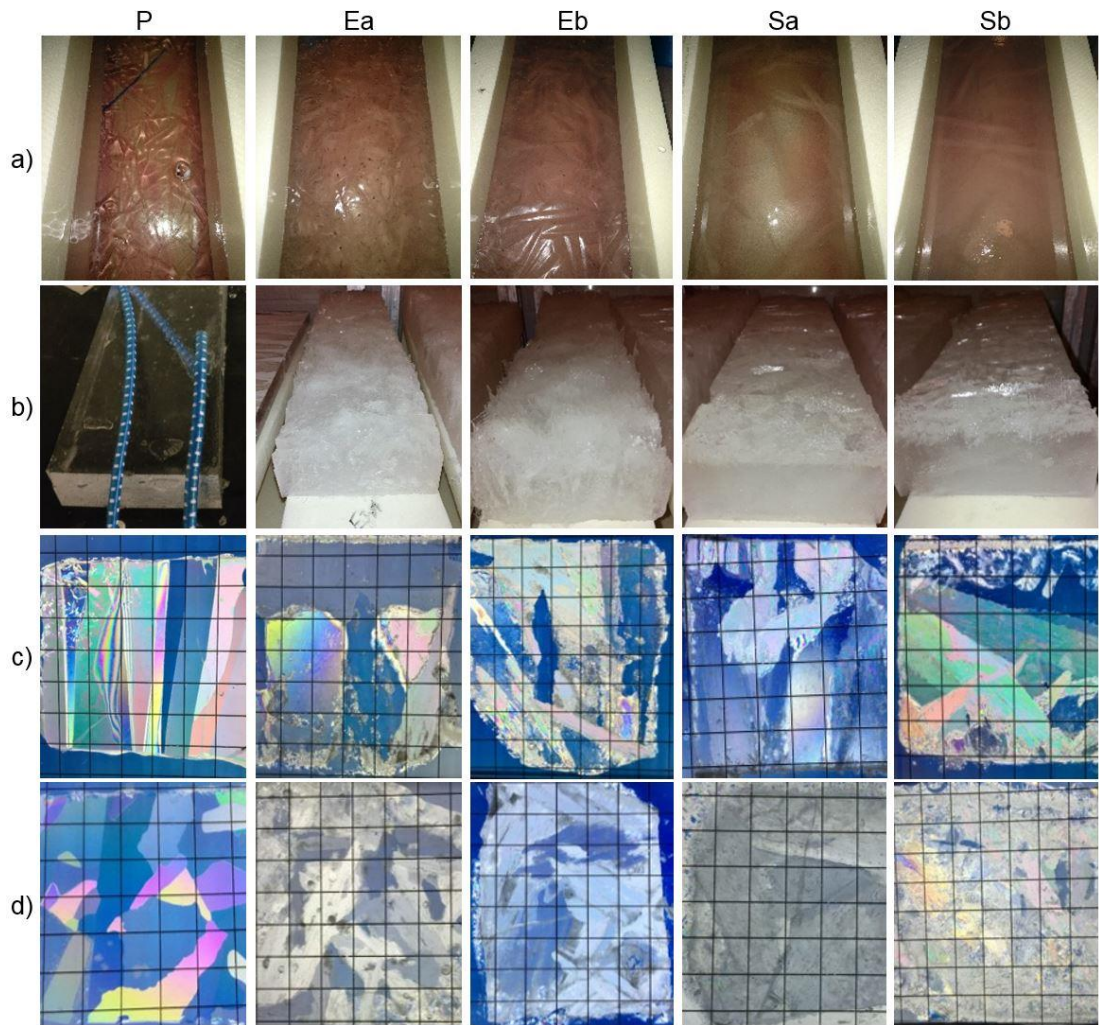
396

397 **Fig. 5** Freezing temperatures and actions conducted during the measurement. Vertical lines represent the removal of  
 398 each row of ice.

399 The samples in row four were taken out after 53 h of freezing at  $-5\text{ }^{\circ}\text{C}$ . However, the samples  
 400 were rather thin (P4 35 mm, E4a 12 mm and E4b 9 mm, S4a 22 mm and S4b 19 mm). The  
 401 S4a and P4 samples were the only ones rigid enough to be hung from the flexural rope for the  
 402 elastic modulus measurements. Then, the ice growth continued in other rows at lower  
 403 temperatures for longer freezing times to produce thicker ice layers for mechanical testing  
 404 purposes. The temperature was first lowered to  $-15\text{ }^{\circ}\text{C}$  for 13 h, and after that raised to  $-10\text{ }^{\circ}\text{C}$ .  
 405 As a result, the samples in row three were taken out after 75 h of freezing, of which 60 h  
 406 was at  $-5\text{ }^{\circ}\text{C}$ , 13 h at  $-15\text{ }^{\circ}\text{C}$  and 2 h at  $-10\text{ }^{\circ}\text{C}$ . The thicknesses of the ice samples were 59 to  
 407 72 mm and the samples were strong enough for the mechanical property tests. To stop the  
 408 ice growth in the two remaining sample rows, the temperature was increased to  $-5\text{ }^{\circ}\text{C}$ . The  
 409 samples in rows two and one were frozen an additional 4.5 and 6 h, respectively, at  $-5\text{ }^{\circ}\text{C}$   
 410 before removal from the freezing boxes.

411 **3.2 Properties of ice**

412 The ice samples could be distinguished from the outlook from the surface of the ice; see row  
413 a) in Fig. 6. From the left, the first column is tap water (P) ice, which was clear and did not  
414 contain any bubbles. The second (Ea) and third (Eb) columns are the ethanol solutions that  
415 had some bubbles and were not fully transparent. The fourth (Sa) and fifth columns (Sb) are  
416 the sodium chloride solution and appear cloudy. After the samples were taken out from the  
417 freezing boxes, they were placed bottom up on an even surface to protect the fragile bottom  
418 ice crystals; see row b) in Fig. 6. After the mechanical properties of the ice were measured,  
419 vertical and horizontal thin sections were prepared from the samples; see rows c) and d) in  
420 Fig. 6.



421

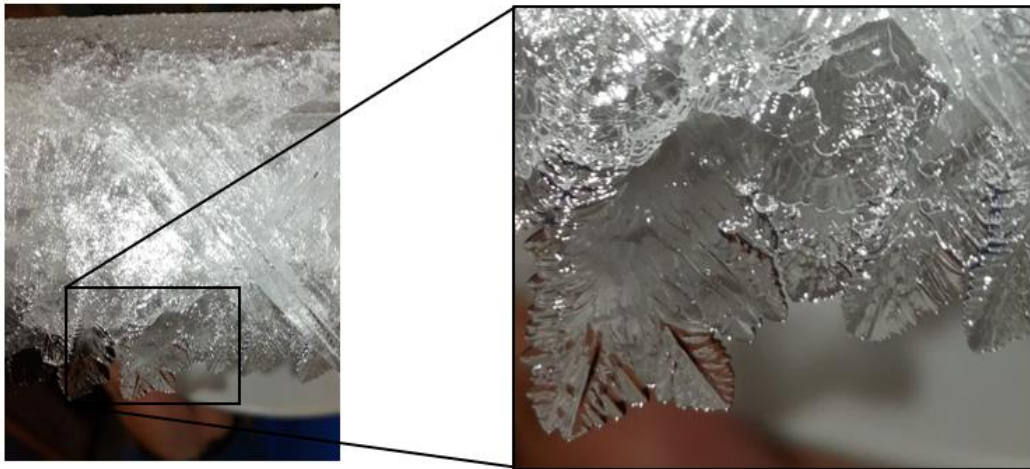
422 **Fig. 6** Pictures of the ice samples (from row three). The columns from left to right are P, Ea, Eb, Sa, and Sb; a)  
 423 the samples in the freezing boxes, b) the samples upside down after recovery, c) vertical thin sections from row two,  
 424 and d) horizontal thin sections from row three. The scale bar is 1 cm x 1 cm.

425 The ice from tap water (P) had the most homogeneous ice crystal structure. The ice samples  
 426 were clearly transparent and the top and bottom surfaces were smooth. The ice structure was  
 427 columnar, with all of the crystals oriented almost vertically; see the vertical thin section in Fig.  
 428 6c) and d). However, the crystal (or grain) size in the horizontal direction varied from 10 to 40  
 429 mm and was irregular. The irregular structure is considered to result from the unseeded origin  
 430 of the ice growth, as earlier studies have shown that ice with a relatively homogeneous grain

431 size can be obtained by seeding with ice crystals (Gow et al., 1988).

432

433 The ice grown from ethanol solutions (Ea and Eb) had the most irregular structure. The ice  
 434 first grew an approximately 9 mm solid layer. After this layer, dendritic crystal platelets started  
 435 to grow. The diameters of the platelets were up to 100 mm, the thickness was up to 5 mm,  
 436 and the orientation appeared to be random. There were distinguished regions between the  
 437 platelets, and many platelets were not connected. Fig. 7 shows the E4b sample after being  
 438 taken out from the freezing box at this stage of the growth.



439

440 **Fig. 7** Close-up of E4b ice structure from the side. On the top, approximately 9 mm of solid ice structure and then  
 441 large dendritic platelets oriented towards the liquid.

442 When the freezing continued, bridges between the platelets started to form, leading to a more  
 443 solid ice structure. However, the bottom of the ice remained irregular and thin sections showed  
 444 that the gaps had not fully closed; see Fig. 6c) and d). Thus, the ice was porous, and in some  
 445 cases, the platelets growing together might have entrapped ethanol solution inside the ice.

446

447 The ice from the sodium chloride solution (Sa and Sb) had a structure between the tap water  
 448 and ice frozen in the ethanol solution. The ice was cloudy and almost opaque. The top surface

449 was smooth but the bottom surface rough. The ice grew in platelets, but thinner and smaller  
 450 in diameter than in the ice obtained from the ethanol solution. The platelets were oriented  
 451 locally in the same direction, see Fig. 6c) and d). The ice was also less porous than the ice  
 452 obtained from the ethanol solution, as the platelets seemed to grow almost at the same rate.  
 453 Thus, the ice formed in the sodium chloride solution was more solid than the ice obtained from  
 454 the ethanol solution.

455

456 Prior to the mechanical and chemical measurements, the physical properties were measured.

457 The average length of the ice samples was 567 mm and the width 143 mm. Table 1 presents

458 the thickness, mass and growth rate of the samples. The chemical and mechanical properties

459 were determined after physical measurements with the procedures described in Section 2.

460 Table 1 and Table 2 present the results of the chemical and mechanical property

461 measurements for each sample, respectively. The average ice layer growth rate ( $\cdot 10^{-7}$  m/s)

462 was calculated by the measured average ice layer thickness formed during freezing time. The

463 average ice mass growth rate ( $\text{g/h}\cdot\text{m}^2$ ) was calculated by the mass of ice layer formed during

464 freezing time per freezing area.

465 **Table 1** Physical and chemical properties of the ice.

	Sample	Ice mass	Thickness	TOC	Conductivity	Calculated molality	Ice layer growth	Ice mass growth
		g	mm	mg/l	$\mu\text{S/cm}$	mol/kg $\text{H}_2\text{O}$	$\cdot 10^{-7}$ m/s	$\text{g/h}\cdot\text{m}^2$
Tap water	P1	5702 (2787 <sup>1a)</sup> )	72 (45.6 <sup>1a)</sup> )	0.7 (3.9 <sup>2)</sup> )	15 (121.8 <sup>2)</sup> )	-	2.46	823
	P2	5224	66	0.2	2.9	-	2.30	769
	P3	4801 (2473 <sup>1a)</sup> )	61 (31 <sup>1a)</sup> )	0.7	6.7	-	2.26	749
	P4	2392	31	0.9	4.0	-	1.65	528
EtOH 0.1 m	E1a	4985	71	1174 (2349 <sup>2)</sup> )	-	0.044 (0.089 <sup>2)</sup> )	2.44	720
	E2a	5079	70	1452	-	0.053	2.44	747
	E3a	4987	66	1207	-	0.045	2.45	778
	E4a	2288	29	629.8	-	0.024	1.53	505
EtOH 0.3 m	E1b	4803	75	2293 (7401 <sup>2)</sup> )	-	0.091 (0.292 <sup>2)</sup> )	2.58	693
	E2b	5095	73	2959	-	0.119	2.56	750
	E3b	4800	72	2594	-	0.103	2.66	749
	E4b	2125	27	2230	-	0.086	1.42	469
NaCl 0.1 m	S1a	5196 (2410 <sup>3)</sup> )	66 (32.95 <sup>3)</sup> )	-	2922 (9610 <sup>2)</sup> )	0.029 (0.104 <sup>2)</sup> )	2.25	750
	S2a	5212	64	-	3010	0.030	2.24	767
	S3a	5067	63	-	2894	0.030	2.34	790
	S4a	2386	29	-	1622	0.015	1.51	526
NaCl 0.3 m	S1b	5071 (2193 <sup>1c)</sup> )	63 (29.8 <sup>1c)</sup> )	-	9285 (26200 <sup>2)</sup> )	0.101 (0.302 <sup>2)</sup> )	2.17	732



S2b	4641	59	-	7580	0.080	2.06	683
S3b	4592	59	-	9620	0.103	2.17	716
S4b	1983	27	-	7710	0.082	1.40	438

<sup>1a)</sup> Mass and thickness of the bottom ice sample when measuring natural frequency

<sup>1b)</sup> Average mass from the top and bottom sections when measuring natural frequency

<sup>1c)</sup> Mass and thickness of the top ice sample when measuring natural frequency

<sup>2)</sup> TOC/conductivity/molality for the initial solution

<sup>3)</sup> Average mass and thickness from top and bottom sections of the natural frequency measurement

466

467 **Table 2** Mechanical properties of the ice.

	Sample	Natural frequency (flexural)	Flexural strength	Dynamic Modulus of elasticity	Static Modulus of elasticity
		Hz	kPa	GPa	GPa
Tap water	P1	580.80 <sup>1a)</sup>	971.00 <sup>1d)</sup>	7.38	-
	P2	601.00	890.00	7.93	1.27
	P3	267.10 <sup>1a)</sup>	1384.50 <sup>1d)</sup>	8.00	6.08 <sup>1d)</sup>
	P4	316.50	1072.00	9.24	4.57
EtOH 0.1 m	E1a	-	366.50 <sup>1d)</sup>	-	-
	E2a	634.50	144.00	7.22	1.12
	E3a	620.00	275.50 <sup>1d)</sup>	7.89	1.26 <sup>1d)</sup>
	E4a	-	-	-	-
EtOH 0.3 m	E1b	-	128.50	-	-
	E2b	-	56.00	-	-
	E3b	-	146.67	-	-
	E4b	-	-	-	-
NaCl 0.1 m	S1a	288.05 <sup>1b)</sup>	581.00 <sup>1d)</sup>	6.82	3.93 <sup>1d)</sup>
	S2a	407.60	202.00	3.95	0.58
	S3a	389.40	438.50 <sup>1d)</sup>	3.69	7.69 <sup>1d)</sup>
	S4a	230.80	248.00	6.83	-
NaCl 0.3 m	S1b	240.50 <sup>1c)</sup>	622.00 <sup>1d)</sup>	5.75	4.12 <sup>1d)</sup>
	S2b	383.00	152.00	3.98	0.57
	S3b	474.50	303.50 <sup>1d)</sup>	6.15	5.09 <sup>1d)</sup>
	S4b	-	-	-	-

<sup>1a)</sup> Natural frequency of bottom ice part

<sup>1b)</sup> Average natural frequency of top and bottom sections.

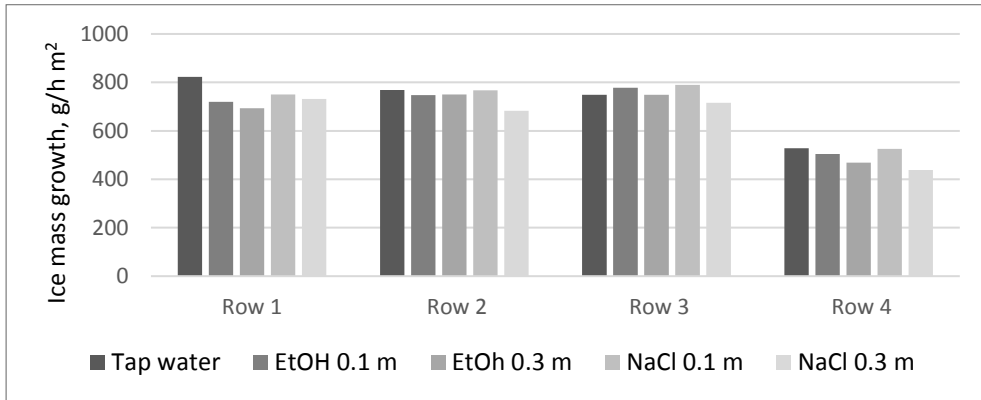
<sup>1c)</sup> Natural frequency of the top ice part

<sup>1d)</sup> Average value from upper and lower part

468

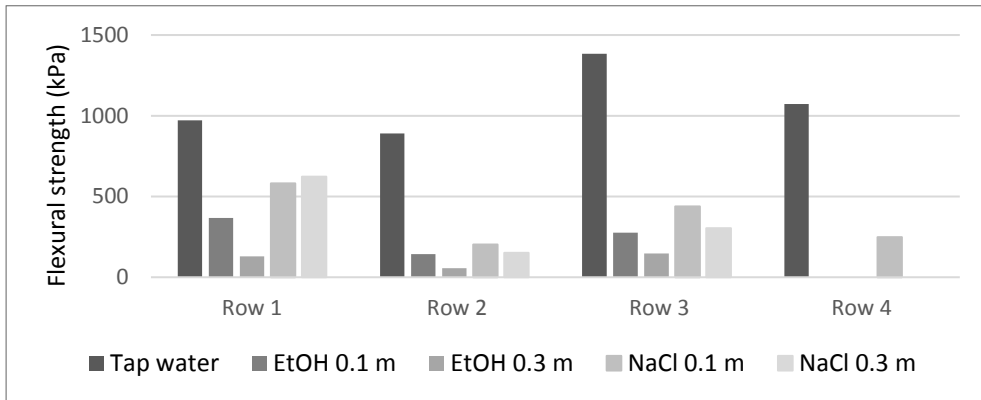
469 Average ice mass growth rates (g/h, m<sup>2</sup>) of measured ice samples are plotted in Fig. 8 and

470 average flexural strength values (kPa) in Fig. 9.



471

472 **Fig. 8** Average ice mass growth rates (g/h m<sup>2</sup>) of measured ice samples.



473

474 **Fig. 9** Average flexural strength values (kPa) of measured ice samples.

475

#### 476 **4 Discussion**

477 In the following section, the average properties of each measurement are calculated from the  
 478 samples of rows one, two and three, and results are compared. The samples of the fourth row  
 479 were taken out first when the amount of ice was still very low and mechanical measurements  
 480 could not be performed with three ice samples out of five.

481 **4.1 Average ice properties of the tap water**

482 Table 3 summarizes the average properties of tap water ice samples one to three. If the  
 483 properties for the top and bottom layer were measured separately, the average of the layer  
 484 measurement was used as a value for the sample. The tap water ice properties were  
 485 measured for reference values to compare the difference in the ice structures grown in ethanol  
 486 and sodium chloride solutions. As the ethanol and sodium chloride were mixed with the tap  
 487 water, the effect on its properties was captured. The average mass of ice that was created  
 488 was 5242 g, and the measured density was 934 kg/m<sup>3</sup>. The natural frequency is related to the  
 489 thickness of the ice, as the width and length of the beams were identical. This gives a value  
 490 for the stiffness of the ice that formed in relation to the thickness of the ice. The higher the  
 491 value for Hz/mm is, the stiffer the formed ice layer is. The modulus of elasticity is calculated  
 492 from the first flexural natural frequency and beam theory (Eq. 1). The static modulus of  
 493 elasticity is calculated from the displacement during the flexural strength test that is based on  
 494 a static test (Eq. 5). In addition, the flexural strength was measured for the created ice samples.  
 495 The ice formed from the tap water has the highest natural frequency per thickness, modulus  
 496 of elasticity and flexural strength; compare Table 3, Table 4 and Table 5.

497 **Table 3** Average ice properties of the tap water samples one to three.

Property	Unit	Tap water
Mass growth rate per unit surface area	g/h m <sup>2</sup>	780
Linear growth rate	m/s	2.34·10 <sup>-7</sup>
Mass	g	5242
Density	kg/m <sup>3</sup>	934
Natural frequency	Hz	483
Thickness	mm	66.33 (47.47) <sup>1)</sup>
Average natural frequency per mech. thickness	Hz/mm	10.17
Dynamic modulus of elasticity	GPa	7.77
Flexural strength	kPa	1082
Static modulus of elasticity	GPa	3.68

<sup>1)</sup> Average thickness from natural frequency measurements

498

499 **4.2 Average ice properties of the ethanol solutions**

500 Table 4 shows the average properties for the ice grown from ethanol solutions. The ice formed  
 501 from the 0.3 mol/kg solution was very weak, and only part of the measurements were possible  
 502 to conduct. Compared to the tap water properties, the ice mass growth rate was lower but the  
 503 ice layer growth rate was higher. The average natural frequency per thickness was lower,  
 504 meaning that the ethanol ice was softer. The flexural strength was significantly lower compared  
 505 to the tap water ice, which is also visible from the modulus of elasticity (static) that was  
 506 determined from the four-point bending test. Table 4 shows that the ice that formed from the  
 507 concentrated ethanol solution is clearly mechanically weaker, as expected. The average  
 508 separation efficiency was 47% with a dilute 0.1 mol/kg ethanol solution and the effective  
 509 distribution coefficient  $K$  was 0.53 (i.e. the ratio between impurity concentrations in the ice and  
 510 in the initial solution), whereas with the concentrated 0.3 mol/kg ethanol solution the obtained  
 511  $K$  was 0.36 and separation efficiency 64%. In this case, the average separation efficiency was  
 512 higher with a more concentrated initial solution.

513 **Table 4.** Average properties of ice obtained with ethanol solution concentrations 0.1 and 0.3 mol/kg.

Property	Unit	Ethanol 0.1 mol/kg H <sub>2</sub> O	Ethanol 0.3 mol/kg H <sub>2</sub> O
Mass growth rate per unit surface area	g/h m <sup>2</sup>	748	731
Linear growth rate	m/s	2.44 · 10 <sup>-7</sup>	2.60 · 10 <sup>-7</sup>
Mass	g	5017	4899
Density	kg/m <sup>3</sup>	907.6	-
Natural frequency	Hz	627	-
Thickness	mm	69 (68.05) <sup>1)</sup>	73.33
Average natural frequency per thickness	Hz/mm	9.21	-
Dynamic modulus of elasticity	GPa	7.56	-
Flexural strength	kPa	262	110
Static modulus of elasticity	GPa	1.2	-
Measured initial impurity molality in solution	mol/kg H <sub>2</sub> O	0.089	0.292
Impurity molality in ice	mol/kg H <sub>2</sub> O	0.047	0.104

<sup>1)</sup> Average thickness from natural frequency measurements

514 **4.3 Average ice properties of sodium chloride solutions**

515 Table 5 shows the average properties for the ice samples formed from 0.1 and 0.3 mol/kg  
 516 sodium chloride solutions. A comparison of Table 3 to Table 5 shows that the values of  
 517 mechanical ice properties and ice growth rates for the sodium chloride solution are smaller  
 518 than for tap water but higher than for the ethanol solution. In general, it was noticed that the  
 519 ice formed from sodium chloride solutions are mechanically harder than the ice formed from  
 520 ethanol solutions. The ice formed from a concentrated 0.3 mol/kg sodium chloride solution  
 521 was mechanically harder (flexural strength 359 kPa) than ice formed from a dilute 0.1 mol/kg  
 522 ethanol solution (262 kPa), even though the impurity concentration of sodium chloride ice was  
 523 double when compared with the concentration of ethanol ice, i.e. 0.095 mol/kg vs. 0.047  
 524 mol/kg, respectively. The separation efficiency was 71% with a dilute 0.1 mol/kg sodium  
 525 chloride solution (and the effective distribution coefficient,  $K$ , 0.29), whereas with a  
 526 concentrated 0.3 mol/kg sodium chloride solution it was 69% (and  $K$  0.31).

527 **Table 5** Average properties of ice obtained with sodium chloride solution concentrations 0.1 and 0.3 mol/kg.

Property	Unit	Sodium chloride 0.1 mol/kg H <sub>2</sub> O	Sodium chloride 0.3 mol/kg H <sub>2</sub> O
Mass growth rate per unit surface area	g/h m <sup>2</sup>	769	710
Linear growth rate	m/s	2.28·10 <sup>-7</sup>	2.13·10 <sup>-7</sup>
Mass	g	5158	4768
Density	kg/m <sup>3</sup>	961	938
Natural frequency	Hz	362	366
Thickness	mm	64.33 (53.35) <sup>1)</sup>	60.33 (49.13) <sup>1)</sup>
Average natural frequency per thickness	Hz/mm	6.78	7.45
Dynamic modulus of elasticity	GPa	4.82	5.29
Flexural strength	kPa	407	359
Static modulus of elasticity	GPa	4.07	3.26
Measured initial impurity molality of solution	mol/kg H <sub>2</sub> O	0.104	0.302
Impurity molality in ice	mol/kg H <sub>2</sub> O	0.030	0.095

<sup>1)</sup> Average thickness from natural frequency measurements

528 **4.4 Comparison between the formed ice and to earlier studies**

529 Table 6 depicts the discovered impurities of ice, ice growth rates and mechanical properties

530 related to properties of tap water ice. The ethanol concentration 0.104 mol/kg in the ice (initial  
 531 solution 0.3 mol/kg) reduced the flexural strength 90% when compared to the flexural strength  
 532 of tap water ice. Sodium chloride concentration 0.095 mol/kg in the ice (initial solution 0.3  
 533 mol/kg) reduced the flexural strength 67%, while a half lower ethanol concentration 0.047  
 534 mol/kg in the ice (initial solution 0.1 mol/kg) generated a 76% strength reduction. Increasing  
 535 the sodium chloride concentration in the ice from 0.030 mol/kg to 0.095 mol/kg did not have a  
 536 very noticeable effect on the mechanical rigidity of the ice. The obtained natural frequency per  
 537 thickness decreased only 9% with 0.047 mol/kg ethanol ice compared to tap water ice. Based  
 538 on the research, the source of impurity is distinguishable from the differences in the natural  
 539 frequencies of the ice beams, i.e. the effective stiffness of the ice is at a specific level.

540 **Table 6** Average properties of ethanol and sodium chloride ice compared to properties of tap water ice, samples from  
 541 rows one to three.

Samples (rows 1 to 3)	Impurity molality mol/kg H <sub>2</sub> O	Layer growth <sup>1)</sup>	Mass growth <sup>1)</sup>	Flexural strength <sup>1)</sup>	Static modulus of elasticity <sup>1)</sup>	Natural frequency/ thickness (mech) <sup>1)</sup>	Dynamic modulus of elasticity <sup>1)</sup>
Tap water (P)	-	1.00	1.00	1.00	1.00	1.00	1.00
EtOH 0.1 m (Ea)	0.047	1.04	0.96	0.24	0.32	0.91	0.97
EtOH 0.3 m (Eb)	0.104	1.11	0.94	0.10	-	-	-
NaCl 0.1 m (Sa)	0.030	0.97	0.99	0.38	1.11	0.67	0.62
NaCl 0.3 m (Sb)	0.095	0.91	0.91	0.33	0.89	0.73	0.68

<sup>1)</sup> Related to tap water ice value

542 The flexural strength results show that tap water ice is the strongest, as expected, and the  
 543 ethanol solution ice is the weakest. This may partly result from the structure of the ice. As  
 544 noted in the method description, the beams were assumed to be solid in the calculation of the  
 545 second moment of inertia as it was not possible to measure the actual porosity. It should be  
 546 noted that, especially, in the case of ethanol ice, the beams were to solid ice through the  
 547 thickness and contained pores. Thus, the determined  $I$  is overestimating the stiffness that  
 548 leads to the underestimation of the flexural strength in these cases. When compared the

549 studied ice conformations, the structure of tap water ice was the most dense (less porous) and  
550 the orientation of the crystals columnar. Ethanol ice had large crystals oriented in different  
551 directions, and there were clear regions between the platelets. Thus, the ice was more porous,  
552 and concentrated ethanol solution might have been entrapped inside the ice when the platelets  
553 were freezing together, i.e. the ice was becoming more dense. The ice from sodium chloride  
554 solutions had a structure between these two – the crystals were oriented less randomly and  
555 the ice was less porous than the ethanol solution ice but not as dense and even-structured as  
556 tap water ice. Thin sections also showed that the crystals of the tap water ice were more  
557 rounded, whereas ethanol solution ice had platelet shaped crystals, and sodium chloride  
558 solution ice crystal shapes were between these two, see Fig. 6c and d.

559

560 When these conducted measurements are compared with the previous studies about naturally  
561 formed ice in lakes, rivers and seas, the results are reasonable. The tap water represents (in  
562 terms of salinity) freshwater ice and the measured values are similar to the values of  
563 freshwater ice. The strength of the sodium chloride solutions is similar to lower values of the  
564 sea ice strength. Also the static and dynamic elastic modulus values of the tap water and  
565 sodium chloride solutions are in the same range as with sea and freshwater ice. The ice grown  
566 from the ethanol solution showed higher values than those obtained with fine grained ethanol  
567 model scale ice as addressed by Riska et al. (1994). This is reasonable due to structural  
568 differences. When the fine grained ethanol ice is produced by spraying, see Von Bock und  
569 Polach et al. (2013) the obtained grain size is 1 mm or smaller and the grains are sphere-like.  
570 The fracture process occurs along the grain boundaries and by having smaller grain sized ice  
571 it leads to weaker ice. Timco (1981)

572

573 Timco (1981) conducted an extensive test series with different aqueous solutions. He noted

574 that the flexural strength decreases as a function of the solute mass fraction increase until a  
575 transition concentration point where the ice strength approaches a constant level. The results  
576 presented in this paper with sodium chloride solutions are consistent with Timco's results. In  
577 the present work, molalities were used for the more accurate comparison of the influence of  
578 organic compounds and inorganic salt on ice properties. In addition to mechanical property  
579 measurements, the thin sections and structure of obtained ice were presented in this paper,  
580 describing the structure of ice more clearly.

581

582 The results show that the average separation efficiency with a 0.3 mol/kg ethanol solution,  
583 64%, is higher than with a 0.1 mol/kg ethanol solution, 47%, whereas separation efficiencies  
584 with both sodium chloride solutions are at the same level, close to 70%. This peculiar  
585 difference in efficiencies could not be noticed within row four ice samples with a higher freezing  
586 temperature (-5°C) and therefore induced lower ice growth rates. The separation efficiency  
587 with the 0.3 mol/kg ethanol solution was 71% and with 0.1 mol/kg 73%, while with a 0.3 mol/kg  
588 sodium chloride solution it was 73% and with 0.1 mol/kg as high as 86%. It is already  
589 recognised that higher separation efficiencies can be achieved with lower ice growth rates and  
590 dilute solutions (Butler, 2002; Hasan and Louhi-Kultanen, 2015), but no clear explanation for  
591 the variation in the ice growth mechanism is known. It might be a result of the structure of the  
592 ice in the intermediate stages, i.e. during the growth process, or due to the different properties  
593 of the organic (EtOH) and inorganic solutions (NaCl). As this is beyond the scope of this paper,  
594 the explanation to this would require additional ice structure studies in relation to ice  
595 crystallization kinetics and thermodynamics.



## 596 **5 Conclusions**

597 The five different initial aqueous solutions – tap water, ethanol and sodium chloride solutions  
598 of molalities 0.1 and 0.3 mol/kg – transformed into visually distinguishable ice structures during  
599 natural air-cooled freezing. The differences were noticeable also in terms of the conducted  
600 chemical and mechanical measurements. Tap water was used as a reference liquid as well  
601 as a solvent in ethanol and sodium chloride solutions to compare the properties of the studied  
602 ice when ice formed from tap water had the highest flexural strength and natural frequency.  
603 The dopants added to the tap water changed the mechanical properties and chemical analysis  
604 results of the ice. The platelet diameter and thickness in the intermediate growth stage were  
605 the greatest and the orientation was the most random for ice formed from ethanol solutions,  
606 which affected the final structure of the ice so that the ethanol ice had the most irregular  
607 structure. Based on the research, the ice formed from the ethanol solution is more fragile than  
608 the ice formed from the tap water, as the flexural strength is much lower than in tap water ice  
609 and sodium chloride ice. Ethanol appeared to weaken the ice more effectively compared to  
610 sodium chloride.

611

612 In summary, the amount of added chemical dopants, ethanol and sodium chloride, was  
613 reduced with variation from 47% to 86% by natural freezing at cooling air temperatures -15°C  
614 and -5°C, respectively. This verifies the assumption that higher separation efficiencies can be  
615 obtained by lower ice growth rates at higher freezing temperatures, but different chemical  
616 characteristics still seem to affect the efficiency level as well. The present study gives a good  
617 basis for further research concerning the development of ice harvesting techniques and  
618 purification efficiency investigations of freeze separation applications with real wastewaters.

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