

**Relation between managerial cognition and industrial performance: An assessment with strategic cognitive maps using fuzzy-set qualitative comparative analysis**

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**Abstract**

Strategic management researchers have long been fascinated with company performance in terms of underlying managerial cognition and its interpretation. This paper presents a methodology to examine the linkage between the cognition of individuals and company performance. We link cognitive maps with fuzzy-set qualitative comparative analysis (fsQCA) and examined the role of standard and newly proposed consistency and coverage formulas in the evaluation of social science data. We investigate the effect of cognitive diversity within a company, and between companies within an industry on company performance using experimental and real-life data. The proposed method used a cognitive mapping approach to elicit strategy frames from individuals in management teams and operationalized their cognitive diversity by distance ratios between individual- and group-level cognitive maps. The results highlight the different opportunities of cognitive diversity to the enhancement of company performance in the market and confirm the usefulness of new fsQCA consistency and coverage measures.

*Keywords:* Cognitive diversity, Cognitive map, Consistency, Coverage, Distance ratio, Performance

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1 **Relation between Managerial Cognition and Industrial**  
2 **Performance: An Assessment with Strategic Cognitive maps**  
3 **using Fuzzy-Set Qualitative Comparative Analysis**

4 **1. Introduction**

5 The ultimate question of strategic management research is why some  
6 companies outperform others. One of the streams of research seeking  
7 answers to this question focuses on cognition in strategic management.  
8 Cognition in strategic management is often conceptualized in terms of  
9 strategic or cognitive frames, which represent cognitive construction  
10 strategies, and the key elements of strategy frames are their content and  
11 structure (Narayanan et al., 2011). Cognitive processes are used when  
12 people generate new knowledge, retrieve older knowledge from memory  
13 (where it has been stored in the form of knowledge structures), and apply  
14 knowledge (e.g., in decision-making). The concepts of strategic cognition  
15 and strategic frames refer to domain-specific cognitive structures and  
16 processes that are applied in a strategic decision-making context  
17 (Narayanan et al., 2011). Cognitive maps are mental representations of  
18 reality that include the central concepts of a domain at issue and the  
19 connections among these concepts. Causal maps are a subgroup of  
20 cognitive maps, essentially describing beliefs of the causal relationships  
21 among domain-specific factors. In this study, we approached cognition by  
22 means of cognitive-mapping techniques and used cognitive maps for the  
23 investigation of cognitive diversity and its effects on performance.

24 In order to take stock of this research of strategic cognition, scholars

25 have presented reviews of this stream, see for example [Kaplan \(2011\)](#) and  
26 [Narayanan et al. \(2011\)](#). [Kaplan \(2011\)](#) organizes research on cognition and  
27 strategy in stages of 1) generating a ‘proof of concept’ (i.e., generating  
28 legitimacy for the line of inquiry), 2) assessing the accuracy of the  
29 managers’ cognitive frames, 3) connecting cognition to strategic outcomes,  
30 and 4) building dynamic models of cognition in strategy making. When  
31 summarizing her review of research on the connection between cognition  
32 and strategic outcomes, [Kaplan \(2011, p. 680\)](#) states that this stream has  
33 shown “not only that managerial cognitive frames exist (‘proof of concept’)  
34 but that they matter.” [Narayanan et al. \(2011\)](#), in turn, recognize five  
35 different streams within the cognitive perspective in strategy: 1)  
36 antecedents and outcomes of strategy frames, 2) determinants and  
37 consequences of strategy formulation, 3) cognitive construction of  
38 competitive/industry dynamics, 4) determinants and consequences of  
39 strategy implementation, and (5) antecedents and outcomes of  
40 organizational identity. They conclude their review on antecedents and  
41 outcomes of strategy frames by noting that the content of strategy frames  
42 is related to the context of the company (i.e., environmental, strategic, and  
43 organizational context) and that the structure of strategy frames matches  
44 the turbulence and dynamism of the environment. Thus, the extant  
45 knowledge finds that strategic cognition is linked to company performance.  
46 According to [Gary and Wood \(2011\)](#), diversity in cognition is generally seen  
47 as a source of heterogeneity in company strategies and performance. Yet, it  
48 is difficult to draw any generalizable conclusions about the nature of this  
49 relationship from the existing research. One way to approach this issue is to

50 operationalize the cognitive frames and the diversity thereof by means of  
51 cognitive maps. [Jenkins and Johnson \(1997\)](#) find that the idiosyncratic  
52 details of the content and the structure of the cognitive maps explain the  
53 relationship between cognition and performance rather than the overall  
54 characteristics of the cognitive maps. These idiosyncratic details in Jenkins  
55 and Johnson's ([1997](#)) study were linkages that included concepts related to  
56 customers, actions and performance measures. Of course, these perceived  
57 causal linkages are not necessarily idiosyncratic (i.e., distinctive) in other  
58 contexts.

59 Thus, one of the main challenges in the study of the linkage between  
60 cognition and performance is that the idiosyncrasy or distinctiveness of  
61 content and the structure of cognition are highly dependent on the context  
62 in which the companies operate. This context dependency makes it difficult  
63 to accumulate evidence that is needed for drawing generalizable  
64 conclusions. Research on cognition in competitive or industry dynamics  
65 finds that competition, industry, and strategic groups within an industry  
66 are also cognitively constructed ([Narayanan et al., 2011](#)). This means that  
67 a cognitive context in the industry is formed by a company-level cognition  
68 that operates within the industry, and company-level cognition should be  
69 studied in relation to its cognitive context at an industry level when  
70 assessing its link to performance. Consequently, the kind of content and  
71 structure of the managerial cognition is idiosyncratic and distinctive and  
72 depends on the cognitive context at an industry level. In this paper, we  
73 studied this idiosyncratic nature of managerial cognition and its  
74 relationship to company performance by operationalizing the differences in

75 the managerial cognition of the companies using their distance to the  
76 industry-level cognition represented by an industry-level cognitive map.

77 A diversity of managerial cognition can also occur within a company.  
78 Strategic management of a company is a complex task, which is often  
79 beyond the cognitive capabilities of one person (Bittner and Leimeister,  
80 2014). In this context, diversity in cognition refers to cognitive diversity  
81 within decision-making groups, which is a necessity for the emergence of a  
82 wider horizon of opportunities for organizational renewal and monitoring in  
83 a competitive environment. However, a potential dark side of this cognitive  
84 diversity is that it may lead to difficulties in reaching consensus, which  
85 slows down decision-making and diminishes organizational responsiveness  
86 to environmental changes (Marcel et al., 2011). We examined the diversity  
87 of managerial cognition within the strategic decision-making group and its  
88 relationship to company performance by operationalizing the diversity as  
89 the average distance of decision-makers' cognitive frames (represented by  
90 cognitive maps) to the common company-level cognition (represented by a  
91 company-level cognitive map). Our findings contribute to the literature on  
92 cognition in strategic management.

93 The linkage between cognition and performance is inherently covered  
94 with uncertainty. So, in order to try to model it, we needed tools that can  
95 handle uncertainty. Fuzzy set theory is suitable area for such tools. Zadeh  
96 (1965) first introduced the concept of fuzzy sets that are able to operate  
97 under uncertainty. After his seminal paper, a great deal of mainly  
98 theoretical work was done in the 1970s and 80s, mostly in the United  
99 States, Europe. and Japan (Dubois and Prade, 1980; Klir and Yuan, 1995).

100 From the mid 1980s, applications started to play a larger role starting with  
101 fuzzy control and automation systems (Mamdani and Assilian, 1975; Takagi  
102 and Sugeno, 1985; Sugeno and Kang, 1988), but covering also other areas of  
103 artificial intelligence including, for example, machine learning (Bezdek,  
104 1981). Fuzzy sets found their way in qualitative comparative analysis  
105 (QCA) by Ragin (1987), by the seminal work (Ragin, 2008, 2006, 2014).  
106 Fuzzy-set QCA (fsQCA) is gaining popularity in many fields not just  
107 sociology, although its use and also the development and critical assessment  
108 of the underlying methodology is still actively pursued in flagship journals  
109 in that field (see e.g., Vis and Dul, 2018; Baumgartner and Thiem, 2017;  
110 Braumoeller, 2017; Mikkelsen, 2017). Its growing popularity can be traced  
111 in practically all other fields of social sciences including strategic  
112 management and business research (Greckhamer et al., 2007; Skarmas  
113 et al., 2014; Gabriel et al., 2018; Santos et al., 2018), organizational research  
114 (Meuer and Rupietta, 2016), and case studies (Schneider and Rohlfing,  
115 2016; Mikkelsen, 2017). A special issue on set-theoretic methods in business  
116 has also recently been published in the *Journal of Business Research*  
117 (Roig-Tierno et al., 2016) with papers covering the use of fsQCA as well.

118 In this paper, we contribute to the line of research on the use of fsQCA  
119 in social sciences by investigating the usefulness of newly proposed  
120 consistency and coverage measures by Stoklasa et al. (2018, 2017) in a  
121 practical setting. We developed and present a methodology to study the  
122 linkage between cognitive diversity and performance. A recent research  
123 work (Wang et al., 2016) has revealed direct and indirect effects of cognitive  
124 diversity on team motivation and creativity. In the current study, the

125 proposed method used a cognitive mapping approach to elicit strategy  
126 frames from individuals in the management teams. The cognitive maps  
127 were aggregated to company- and industry-level cognitive maps. The  
128 cognitive diversity of the companies was operationalized as the distance  
129 between the company-level cognition and the industry-level cognition,  
130 which related the company's strategic cognition to its cognitively  
131 constructed context. The effect of the within-company cognitive diversity  
132 on the company's performance was also studied. The links between  
133 cognition and performance were assessed with a fuzzy-set theoretic  
134 qualitative comparative analysis. We demonstrated the method with data  
135 from graduate students competing in teams in an eight-week business  
136 simulation task, which constituted a controlled experiment-like setting for  
137 the investigation of the links among various types of cognitive diversity and  
138 the performance of the companies. We also present the results calculated  
139 for data gathered through a survey from actual managers in the selected  
140 companies in a sustainability business context in Finland that constitutes a  
141 representative sample of the Finnish cleantech industry.

## 142 **2. Data and methods**

### 143 *2.1. Data*

144 The present study represented individual and shared cognitive  
145 structures (strategy frames) in the form of cognitive maps. Data were  
146 collected from two distinct sources: (1) a business simulation task in a  
147 controlled setting was repeatedly performed with graduate students of a  
148 business-oriented program (students represented virtual managers and



149 formed managerial teams) and (2) a survey among the managers of a  
150 representative sample of the companies constituting the Finnish cleantech  
151 industry. Cognitive maps were extracted from both sources to represent the  
152 individual strategy frames. These maps were subsequently fused into a  
153 cognitive map representing a particular company (i.e., the strategy frame of  
154 the company or of the managerial team representing the company in the  
155 simulation task), and the diversity of the team (within-company diversity)  
156 was computed from these maps using two different distance ratios. The  
157 diversity among the companies within the industry was also assessed using  
158 the chosen distance ratios from the cognitive maps. After this, we examined  
159 the relation between performance and diversity using the fsQCA-based  
160 methods.

161 The shared cognitive map data from the strategic management teams,  
162 composed of graduate (Master's degree) students, were collected during an  
163 eight-week business simulation task on strategy implementation. The  
164 simulation was designed to help students understand and interpret the  
165 operations of international trading strategies in global business in a  
166 dynamic and competitive environment. The cognitive maps were developed  
167 based on 40 strategic-level constructs (see Table B.10 in the Appendix).  
168 From this list, each member of the group selected 12 constructs seen as the  
169 most relevant from his/her knowledge and unique views on the situation to  
170 create the cognitive maps. In the data, there were 431 individual-level  
171 cognitive maps which were produced at the beginning and end of the year  
172 (for three years: 2014, 2015, and 2016)<sup>1</sup>. For the purposes of this study, we

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<sup>1</sup>Converted cognitive maps can be found from <https://github.com/luukka76/>

173 analyzed the cognitive diversity at the group (or company) level. To be  
174 able to do so, all the individual maps were converted into association  
175 matrices. The 40 strategic issues plus the total cumulative returns defined  
176 each dimension of the matrix (i.e.,  $41 \times 41$  association matrices were used  
177 to represent each individual map), and the average matrices for each group  
178 were then considered as a representation of the group (or company) level.  
179 To examine the relationship between cognitive diversity in the maps and  
180 the group (company) performance, the total cumulative shareholder return  
181 (TCSR; the 41st column/row in the matrices) was used as an indication of  
182 the group's performance.

183 Data collected from the companies followed the same structure as the  
184 student data. Nine cleantech companies from Finland were included in the  
185 study. In each company, the board of directors provided their interpretations  
186 on causal relations on economic, environmental, and sustainability issues.  
187 The number of members participating from each company varied from three  
188 to seven. To elicit the cognitive maps conceptualizing the strategic knowledge  
189 on the sustainability management, 50 strategic issues were considered. The  
190 company performance was measured using the net profit values that were  
191 collected along with other financial statistics of the selected companies. A  
192 detailed description regarding this data can be found in the publication of  
193 [Bergman et al. \(2020\)](#).

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[Cognitive-maps/blob/master/Cognitive\\_maps/Maps%20-%20data.zip](#)

194 *2.2. Introduction to cognitive mapping*

195 The method of cognitive mapping is one of the most popular techniques  
196 for examining an individual's perceptual representations in strategic  
197 decision-making (Axelrod, 1976). A *cognitive map* is a map defined as a  
198 mental image representing the features of an environment (Kichin, 1994). A  
199 cognitive map can also be denoted by different names depending on the  
200 particular area of research (e.g., a causal map, cause-and-effect diagram, a  
201 strategy map, etc.). Cognitive mapping relates to an individual's daily life;  
202 it is a mechanism shaped by a series of continuous psychological  
203 transformations that include acquiring, coding, decoding, storing, and  
204 recalling information about its relative locations and attributes (Downs and  
205 Stea, 1973). A *directed graph* in graph theory (Bondy and Murty, 1976) has  
206 been used to describe the topology of a cognitive map. The directed graph  
207 consists of a set of vertices (nodes) and a set of directed edges (i.e.,  
208 connections between pairs of nodes that have a clearly identified start- and  
209 end-node). The direction of an edge is usually denoted by an arrow. Robert  
210 Axelrod originally produced a directed graph including causal relations of  
211 an individual and referred to it as a cognitive map (Schneider and  
212 Wagemann, 2012). The nodes in the map represent the variables, and the  
213 edges with arrowheads indicate the directional (causal) relationships among  
214 the variables. The arrowhead represents the direction of the impact, or that  
215 one variable influences another. Cognitive maps can be represented by  
216 weighted directed graphs. In these weighted graphs, the edges are assigned  
217 numerical values (weights) that represent the strength of the assumed  
218 impact or influence.

219 The relationship between two cases (events represented by the nodes in  
220 the graph) such that one causes the other is defined as causality. In  
221 cognitive science, the causality is a critical aspect that plays a crucial role  
222 in decision-making and often supports choosing a course of action that  
223 seems best to achieve the expected outcomes (Carvalho and Tome, 2000).  
224 In the business simulation task with students, individuals were instructed  
225 to draw the cognitive maps by evaluating the impacts of each of the specific  
226 12 strategic issues and TCSR (represented by nodes of the directed graph)  
227 on other selected strategic issues (that is, demonstrate the causal effect  
228 relations with strength and direction). The linkage (edge) between two  
229 nodes represented the direction of the effect, and its weight the strength of  
230 the causality. The effect might be positive (+) or negative (-), and its  
231 strength could be one (weak), two (moderate), or three (strong) (Gerard  
232 et al., 2004). In this case, positive and negative weights of edges were taken  
233 into account when an increase of the causal variable decreased the effect  
234 variable, and when an increase of the causal variable increased the effect  
235 variable, respectively. An example of a cognitive map, including positive  
236 and negative causal relationships between the elements with assigned  
237 strength values, is presented in Figure B.1.

238 [Figure 1 about here.]

239 In an organizational setting, cognitive mapping is an essential tool for  
240 managers who wish to develop complex systems in the fields of strategy  
241 (Kaplan and Norton, 2004; Marshall, 2013), quality (Evans, 2005), business  
242 (Ferreira et al., 2015, 2016) and information systems (Nelson et al., 2000).

243 Typically, managers or companies can apply cognitive maps to achieve  
 244 organizational goals by identifying critical control points and root causes of  
 245 a problem; they can also be used to guide risk management and  
 246 communication strategies and identify causal relations in a complex system  
 247 (Scavarda et al., 2006). However, those people are still suffering from a lack  
 248 of tools and approaches in cognitive analysis. In this study, we intended to  
 249 provide such a method for the analysis of the diversity of managerial  
 250 cognition and for the examination of its relationship to the companies'  
 251 performance.

### 252 2.3. Distance ratio measures for analyzing cognitive maps

253 The examination of the cognitive maps required measuring the cognitive  
 254 diversity among the individual cognitive maps and also the diversity among  
 255 the company-level cognitive maps and the industry-level one. We used the  
 256 distance ratio (DR) as an estimator of cognitive difference between any pair  
 257 of maps. The distance ratio is a value between 0 and 1, and when DR is 1,  
 258 the distance between the maps is at its maximum; whereas when DR is 0,  
 259 the maps are identical (Markoczy and Goldberg, 1995). In this research, we  
 260 first employed the distance ratio formula originally used by Langfield-Smith  
 261 and Wirth (1992, eq. 12), which can be stated as follows:

$$DR_1(A, B) = \frac{\sum_{i=1}^p \sum_{j=1}^p |a_{ij}^* - b_{ij}^*|}{6p_c^2 + 2p_c(p_{u_1} + p_{u_2}) + p_{u_1}^2 + p_{u_2}^2 - (6p_c + p_{u_1} + p_{u_2})} \quad (1)$$

262 where

$$a_{ij}^* = \begin{cases} +1 & \text{for } 0 < a_{ij}, i \text{ or } j \notin P_c \\ -1 & \text{for } 0 > a_{ij}, i \text{ or } j \notin P_c \\ a_{ij} & \text{otherwise} \end{cases} \quad \text{and } b_{ij}^* = \begin{cases} +1 & \text{for } 0 < b_{ij}, i \text{ or } j \notin P_c \\ -1 & \text{for } 0 > b_{ij}, i \text{ or } j \notin P_c \\ b_{ij} & \text{otherwise} \end{cases}$$

263 and  $A$  and  $B$  are two cognitive maps represented by their association  
 264 matrices,  $p$  is the total number of possible nodes representing the strategic  
 265 concepts in a map ( $p$  is the same for both  $A$  and  $B$ ),  $P_c$  is the set of  
 266 common nodes to both maps,  $p_c$  is the number of elements of  $P_c$ ,  $p_{u_1}$  is the  
 267 number of nodes unique to map  $A$ ,  $p_{u_2}$  is the number of nodes unique to  
 268 map  $B$ , and  $a_{ij}$  and  $b_{ij}$  are elements of the  $i^{th}$  row and  $j^{th}$  column in the  
 269 association matrices relative to map  $A$  and  $B$ , respectively. Applying  
 270 different distance ratio measures may provide other options for examining  
 271 the cognitive structures. We also applied a new distance ratio measure that  
 272 was recently introduced by [Bergman et al. \(2020\)](#) as an enhancement of the  
 273 one presented in Equation (1). This generalization was presented by adding  
 274 unit area information, in other words,  $d(x, y) = 1$  cannot be exceeded, by  
 275 taking into account the number of non-zero elements in both maps as  
 276 follows:

$$DR_2(A, B) = \frac{\sum_{i=1}^p \sum_{j=1}^p |a_{i,j}^* - b_{i,j}^*| + |A_a - B_a|}{6p_c^2 + 2p_c(p_{u_1} + p_{u_2}) + p_{u_1}^2 + p_{u_2}^2 - (6p_c + p_{u_1} + p_{u_2}) + T_2} \quad (2)$$

277 where  $A_a$  and  $B_a$  are the counts of non-empty nodes in the cognitive map  $A$   
 278 and  $B$ , respectively and  $T_2 = \max([A_a, B_a])$ . The formulas of  
 279 [Langfield-Smith and Wirth \(1992\)](#) and also [Markoczy and Goldberg \(1995\)](#)

280 have been widely used by managerial and organizational cognition  
281 researchers and easier-to-use tools have been developed like cognizers  
282 (Clarkson and Hodgkinson, 2005) to do the analysis. Since we were also  
283 using the modified form from Bergman et al. (2020) and applying fsQCA,  
284 we used the MATLAB<sup>TM</sup> software and made our own codes to perform the  
285 analysis.

#### 286 *2.4. Fuzzy set-theoretic Qualitative Comparative Analysis*

287 Our analytic approach was based on the fuzzy set-theoretic qualitative  
288 comparative analysis (fsQCA), as we already identified the expected  
289 outcome, input attributes, and cases and performed the first step involving  
290 the calculations of the distance ratios. fsQCA was initially introduced by  
291 Ragin (2000, 2008) and built upon fuzzy set theory for linguistics analysis  
292 from data which were connected with the cases. fsQCA is a powerful  
293 approach that applies a holistic perspective to acquire similarities and  
294 differences through the cases. In fsQCA, an analysis of a set of relations is  
295 produced that conceptualizes the arguments while keeping the uniqueness  
296 of the characteristics and makes comparisons between predictors and the  
297 outcomes (Haumann et al., 2015). Having identified which conditions are  
298 necessary or sufficient to produce the outcome, the fsQCA interprets causal  
299 relationships (cause-effect) between predictor and outcome (Skaaning,  
300 2011). In the set-theoretic framework, the interpretations of set relations  
301 are often made in terms of necessary or sufficient conditions for the  
302 investigated outcome. Necessary and sufficient conditions for an outcome  $B$   
303 can be investigated by examining the consistency and coverage of the  
304 relations  $A \rightarrow B$  and  $B \rightarrow A$  (this is inline e.g., with Schneider and

305 [Wagemann \(2012\)](#)). The consistency of  $A \rightarrow B$  describes how much the  
306 data suggests that  $A \subseteq B$ , in other words, how plausible it is to assume  
307 that  $A$  is a sufficient condition for  $B$ . On the other hand, the consistency of  
308  $B \rightarrow A$  (which is identical with the coverage of  $A \rightarrow B$ ) describes how  
309 much evidence there is in the data for  $B \subseteq A$ , in other words, how plausible  
310 it is to assume that  $A$  is a necessary condition for  $B$  based on the data.  
311 Various consistency and coverage measures are discussed in detail in the  
312 following sections. Using these measures, we intended to apply the fsQCA  
313 to evaluate relationships between various levels of cognitive diversity and  
314 performance. Before we explain the critical aspects of the fsQCA which  
315 were used in this analysis, let us first introduce the basic concepts and  
316 notations of fuzzy set theory, which were used throughout the study.

#### 317 *2.4.1. Basics of fuzzy set-theory*

318 Fuzzy set theory was initially introduced by [Zadeh \(1965\)](#). A *fuzzy set*  $A$   
319 is defined on a non-empty set (universal set)  $U$  by a mapping  $\mu_A : U \rightarrow [0, 1]$ ,  
320 where  $\mu_A$  is called a membership function of  $A$ . For any  $x \in U$ , the value  
321  $\mu_A(x) = A(x)$  is called a degree of membership of  $x$  to fuzzy set  $A$ . A  
322 fuzzy set usually integrates qualitative and quantitative assessments. For  
323 example, the qualitative terms “fully out” and “fully in” are represented by  
324 0 and 1, respectively, and the values in between them represent the partial  
325 membership of a given observation in the fuzzy set. Moreover, there are many  
326 types of fuzzy sets that are characterized by different membership functions.  
327 A triangular-shaped membership function is the simplest and most common  
328 function in current applications. For the real parameters  $\alpha$ ,  $\beta$ , and  $\gamma$  such  
329 that  $\alpha < \beta < \gamma$ , the triangular membership function  $\Lambda(x; \alpha, \beta, \gamma)$  is defined



330 as:

$$\mu_A(x) = \Lambda(x; \alpha, \beta, \gamma) = \begin{cases} 0 & \text{if } x < \alpha \text{ or } x > \gamma \\ \frac{x-\alpha}{\beta-\alpha} & \text{if } \alpha \leq x \leq \beta \\ \frac{\gamma-x}{\gamma-\beta} & \text{if } \beta \leq x \leq \gamma \end{cases} \quad (3)$$

331 Moreover, a trapezoidal membership function  $\Pi(x; \alpha, \beta, \gamma, \delta)$  that is  
 332 formed by four input parameters  $\alpha, \beta, \gamma$ , and  $\delta$  such that  $\alpha < \beta < \gamma < \delta$ , is  
 333 defined as follows:

$$\mu_A(x) = \Pi(x; \alpha, \beta, \gamma, \delta) = \begin{cases} 0 & \text{if } x < \alpha \text{ or } x > \delta \\ \frac{x-\alpha}{\beta-\alpha} & \text{if } \alpha \leq x \leq \beta \\ 1 & \text{if } \beta \leq x \leq \gamma \\ \frac{\delta-x}{\delta-\gamma} & \text{if } \gamma \leq x \leq \delta \end{cases} \quad (4)$$

334 Furthermore, fuzzy sets can be generated by using linguistic labels, for  
 335 example, low, middle, and high, which describe a specific variable called a  
 336 fuzzy variable (Klir and Yuan, 1995). We could say accordingly that the  
 337 analysis in this study was based on the triangular fuzzy sets formed by  
 338 linguistic levels on the distance ratios and performance measures. The  
 339 cardinality of a fuzzy set  $A$  on a finite universal set  $U$  is  
 340  $Card(A) = \sum_{x \in U} \mu_A(x)$ , and on an infinite universal set  $U$ , it is  
 341  $Card(A) = \int_U \mu_A(x) dx$ .

#### 342 2.4.2. Consistency and coverage measures applied in the analysis

343 In the fsQCA, we can calibrate the variables (often addressed from the  
 344 fuzzy sets) using the evidence from the cases and theoretical knowledge  
 345 (Ragin, 2008). In the fsQCA, there are two essential notions, consistency

346 and coverage. Let us assume that we are interested in the assessment of the  
 347 causal relationship  $A \rightarrow B$  using the data we have available. We can be  
 348 interested in knowing whether  $A$  is a sufficient condition for  $B$  (this would  
 349 correspond with  $A \subseteq B$ ) and whether  $A$  is a necessary condition for  $B$   
 350 (which corresponds with  $B \subseteq A$ ). Consistency provides a measure of  
 351 evidence in favor of the investigated claim (e.g.,  $A \subseteq B$ ) in the data, in  
 352 other words, it is dependent on the proportion of cases of  $A$  coinciding with  
 353  $B$  in all cases of  $A$  in the data. If the consistency score is low for a causal  
 354 configuration, then the empirical evidence does not support the existence of  
 355 the given causal configuration (alternatively, we can conclude that the  
 356 presence of  $A$  is not sufficient for the outcome  $B$  to appear). The coverage  
 357 of  $A \rightarrow B$ , on the other hand, indicates how many of the cases of the  
 358 outcome  $B$  are explained by (associated with)  $A$  (Schneider and  
 359 Wagemann, 2012). In contrast to the consistency of sufficient conditions, if  
 360 the amount of coverage is low for a setting, this does not imply less  
 361 relevance (Kane et al., 2014; Tierno et al., 2017).

362 In this analysis, we mainly focused on the consistency and coverage  
 363 measures as defined by Ragin (2008), denoted with an F1 subscript, and  
 364 their enhancements as proposed by Stoklasa et al. (2017, 2018), denoted  
 365 with F2 and F4 subscripts. The original consistency and coverage measures  
 366 are calculated in the following way:

$$Cons_{F_1}(A \Rightarrow B) = \frac{Card(A \cap B)}{Card(A)} = \frac{\sum_{i=1}^n \min(A(x_i), B(x_i))}{\sum_{i=1}^n A(x_i)} \quad (5)$$

$$Cove_{F_1}(A \Rightarrow B) = \frac{Card(A \cap B)}{Card(B)} = \frac{\sum_{i=1}^n \min(A(x_i), B(x_i))}{\sum_{i=1}^n B(x_i)} \quad (6)$$

368 where  $A$  and  $B$  are two fuzzy sets on a universal set  $U = \{x_1, x_2, \dots, x_n\}$ .  
 369 Here, we assume that  $Card(A) \neq 0$  and  $Card(B) \neq 0$  with respect to the  
 370 relation  $A \Rightarrow B$ . When  $A \cap B = A$ , then  $Cons_{F_1}(A \Rightarrow B) = 1$  (perfect  
 371 consistency), and this means that there is no counter-evidence to the given  
 372 relation  $A \Rightarrow B$  in the data. On the other hand,  $Cove_{F_1}(A \Rightarrow B) = 1$   
 373 indicates that only  $A$  is connected with  $B$  in the data (i.e.,  $B \subseteq A$ ). If  
 374 there are other causes for  $B$ , the values of the coverage would be less than 1.  
 375 In general, the idea must be to obtain a good balance in a situation where  
 376 the solution is compelling both theoretically and empirically, and there are  
 377 ranges of consistency and coverage scores that validate our solution. If we  
 378 have very high consistency, but the coverage is low, then our solution is not  
 379 compelling since that does not explain many cases at all (Elliot, 2013). On  
 380 the contrary, if we have a very high coverage but with low consistency, then  
 381 that is also not compelling because there is not enough evidence in favor of  
 382 the case we evaluated.

383 Furthermore, while evidence is being explored in favor of or against  
 384  $A \Rightarrow B$  using set-theoretical concepts, it would be an advantage to examine  
 385 evidence simultaneously to  $A \Rightarrow \bar{B}$ , as suggested by Stoklasa et al. (2017).  
 386 This way we can also take into consideration possible ambivalence in the  
 387 data. To take counter-evidence into account, we can use the formulas for  
 388 fuzzified consistency and coverage measures introduced in Stoklasa et al.  
 389 (2017, 2018) and denoted with an  $F_2$  subscript, which are defined as follows:

$$Cons_{F_2}(A \Rightarrow B) = \frac{\sum_{i=1}^n \min(A(x_i), B(x_i)) - \min(A(x_i), B(x_i), \bar{B}(x_i))}{\sum_{i=1}^n A(x_i)} \quad (7)$$

$$Cove_{F_2}(A \Rightarrow B) = \frac{\sum_{i=1}^n \min(A(x_i), B(x_i)) - \min(B(x_i), A(x_i), \bar{A}(x_i))}{\sum_{i=1}^n B(x_i)} \quad (8)$$

390 From the definition, the  $F_2$  set-theoretic measures take values ranged  
 391 in  $[0, 1]$  where 1 describes the clear evidence (no ambivalence, no counter-  
 392 evidence) and 0 describes the cases in which all the data that provide evidence  
 393 in favor of  $A \Rightarrow B$  also provide at least as strong evidence in favor of  $A \Rightarrow \bar{B}$   
 394 (Stoklasa et al., 2017). This property reduces the values of consistency and  
 395 coverage, and considering all the measures together, they vary according to  
 396 the following rules:

$$Cons_{F_1}(A \Rightarrow B) \geq Cons_{F_2}(A \Rightarrow B) \ \& \ Cove_{F_1}(A \Rightarrow B) \geq Cove_{F_2}(A \Rightarrow B) \quad (9)$$

397 To access the considerable amount of support that we can observe to the  
 398 given relation and to reflect this in the values of the consistency and coverage  
 399 measures, Stoklasa et al. (2017) also have suggested different versions of (7)  
 400 and (8) as  $F_3$  consistency and coverage measures (by reflecting the ambivalent  
 401 evidence again and considering the pure counter-evidence of the investigated  
 402 relationship in the data). Shortly after this, an updated version of these  
 403 measures was suggested (Stoklasa et al., 2018) and denoted as  $F_4$  consistency  
 404 and coverage. Since the latter measures are an extension of the former ones,  
 405 the  $F_4$  measures were considered further in this paper. Stoklasa et al. (2018)  
 406 introduced the  $F_4$  consistency and coverage measures in such a way that  $F_4$   
 407 consistency higher than 0.5 supports the existence of a given relationship. To  
 408 be more precise,  $Cons_{F_4}(A \Rightarrow B) > 0.5$  implies that there is more evidence  
 409 in favor of the given relationship  $A \Rightarrow B$  than there is evidence in favor of

410  $A \Rightarrow \bar{B}$  in the data. In this study, we also employed  $F_4$  measures <sup>2</sup> and their  
 411 formulations were as follows:

$$Cons_{F_4}(A \Rightarrow B) = \frac{1}{2} \left( 1 + \frac{\sum_{i=1}^n \min(A(x_i), B(x_i)) - \min(A(x_i), \bar{B}(x_i))}{\sum_{i=1}^n A(x_i)} \right) \quad (10)$$

$$Cove_{F_4}(A \Rightarrow B) = \frac{1}{2} \left( 1 + \frac{\sum_{i=1}^n \min(A(x_i), B(x_i)) - \min(B(x_i), \bar{A}(x_i))}{\sum_{i=1}^n B(x_i)} \right) \quad (11)$$

## 412 2.5. Research setting

413 Our goal was to examine the impacts of the cognitive diversity on the  
 414 company performance through the analysis of strategic interpretations in  
 415 the cognitive maps. In addition to that, the research model was designed  
 416 based on the information acquired from the cognitive maps where  
 417 individuals' beliefs in a strategic operation have been asserted, and the  
 418 performance measures observed. Initially, we assumed that the different  
 419 levels of diversity of an individual's (managerial) cognition drive the  
 420 company performance. Moreover, we specified these assumptions precisely  
 421 (as described in the next section) to identify the different configurations of  
 422 cognitive diversity that resulted in successful company performance. We  
 423 also considered another source of cognitive diversity, the diversity on the  
 424 company-industry level. The effect of this diversity (the difference of the

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<sup>2</sup>Matlab functions for these measures can be found from <https://se.mathworks.com/matlabcentral/fileexchange/63988-degree-of-support-disproof-consistencies-coverages>

425 company strategic frame from the industry-level one) on the performance of  
426 the company was investigated in an analogous way as the within-company  
427 diversity effect.

### 428 *2.5.1. Hypothesis models*

429 Concerning the data samples, the argument initially built was that the  
430 distance ratio (diversity) between the strategic decision-makers within the  
431 company reflected the group performance. The purpose of this was to develop  
432 and test the hypotheses which determined the relations between cognitive  
433 diversity within the company and the company performance. Next, we also  
434 considered the distances from the group maps (simulating company-level  
435 strategy frames) to the class map (simulating the industry-level strategy  
436 frame), where the class map was created by aggregating all the group maps  
437 in a particular period in a year. This kind of aggregation has previously  
438 been introduced in [Bergman et al. \(2016\)](#). The company-level maps and  
439 the industry-level map were created in an analogous way with the real-life  
440 company data as well; the distance ratio from the company-level maps to the  
441 industry-level map was considered as the diversity among companies within  
442 an industry. In addition, for all the cases, we initially adopted professional  
443 linguistic levels (high, middle, and low) on the variables ( $DR$  and company  
444 performance) and proposed nine hypotheses, as described in [Table B.1](#), to test  
445 the influences of the  $DR$  on the company performance. As an example,  $H_{01}$   
446 in [Table B.1](#) indicates that if the  $DR$  is low, then the company performance  
447 is hypothesized to also be low. Based on the available previous research on  
448 the effects of diversity on performance, we assumed that  $H_{03}$  and  $H_{09}$  would  
449 be supported by the data.

[Table 1 about here.]

### 2.5.2. Process of empirical assessment

The analysis of data started by creating group cognitive maps (i.e., the averaged cognitive maps from all the individuals' maps for each specific group). Such a group map is represented by an average adjacency matrix of the individuals' adjacency matrices (see for example, Table B.11 in the Appendix) of all causal combinations among the elements throughout each of the individual maps. In the next phase, we computed the distance ratios ( $DR_1$  &  $DR_2$ ) from individual maps to group maps using Equations (1) and (2), respectively. The purpose of the use of an additional measure ( $DR_2$ ) was to find more evidence in favor of conclusions driven by the results of the  $DR_1$  measure. To examine how the diversity between the group maps and the class map affected group performance, both the  $DR_1$  and  $DR_2$  distances were used. For the company data, first, all the board members' individual cognitive maps were aggregated to a company-level map for each company, and also individual cognitive maps in all companies were aggregated to the industry-level map. Next, the  $DR_1$  and  $DR_2$  distances were computed from the company's map to the industry-level map and also from the individual cognitive maps to their respective company-level ones.

Once the distance ratios were computed, we moved forward to evaluate the hypotheses. The principal of testing whether a particular hypothesis was rejected or not was based on the context of fuzzification. Fuzzification is a method of transforming exact inputs (crisp inputs) into fuzzy inputs to produce the outcomes based on the fuzzy values (Timothy, 2010, chap.4). The criteria to form the triangular fuzzy sets were based on the linguistic

475 labels high, middle, and low and on the values of the distance ratios and  
476 performance measures. Notice that the choice of these linguistic scales was  
477 based on substantive knowledge to exhibit reasonable characteristics.  
478 Accordingly, membership degrees to the group results were calculated  
479 through the triangular membership function by putting three inputs  
480 selected as the minimum, middle, and maximum values of a given distance  
481 ratio (diversity) and performance measure. The membership degrees were  
482 also categorized into high, middle, and low, and according to the definition  
483 of the membership function, we can notate them as:

484 •  $\mu_{low} \sim \Lambda(x; \alpha, \alpha, \beta),$

485 •  $\mu_{mid} \sim \Lambda(x; \alpha, \beta, \gamma),$

486 •  $\mu_{high} \sim \Lambda(x; \beta, \gamma, \gamma),$

487 where  $\alpha$  is the minimum of the respective values,  $\gamma$  is the maximum of the  
488 respective values, and  $\beta = \frac{\alpha + \gamma}{2}$ . We note here that the performance measure  
489 (total cumulative shareholder return values for each group of students) was  
490 taken as an external piece of information from the study and not from the  
491 cognitive maps.

492 We had the opportunity to collect data repeatedly in the experimental  
493 setting of the business simulation course. Since the setting was similar in all  
494 the runs of the course, we were able to pool all the observations into a single  
495 set of observations to achieve more robustness for our findings; note that the  
496 diversity and performance had to be assessed respective to each simulation  
497 run in this context to avoid unnecessary bias in the analysis. This way, we  
498 obtained the membership degrees of all observations to the respective fuzzy



499 sets representing diversity (high-middle-low) and performance (high-middle-  
500 low). We also obtained a data set with the real-life company data for the  
501 Finnish cleantech industry. For each of the investigated rules summarized  
502 in Table B.1, we calculated the standard fuzzy  $F_1$  consistency and coverage  
503 measures; additionally, the  $F_2$  and  $F_4$  measures were computed to take into  
504 account all the evidence in favor of or against the relations we investigated.  
505 In an analogous way, the fsQCA approaches were applied in the analysis of  
506 the diversity among the group and class maps to the group performance.

507 The first intention of the use of company data in this research was to  
508 show how the proposed method described the relation between the actual  
509 managerial cognition and company performance. Secondly, we also wanted  
510 to investigate the validity of the claims on the managerial cognition and  
511 resulting performance based on the student data sample obtained in a  
512 controlled setting of a classroom business simulation with the data from the  
513 actual managers and companies. Our analysis evaluated the hypotheses  
514 defined in Table B.1 based on the consistency and coverage measures  
515 computed from the  $DR_1$  and  $DR_2$  distance ratios. The analysis of the  
516 company data was done in direct analogy to the analysis of the student  
517 data. The net profit values were considered as performance measures with  
518 the company data, which were collected with other financial statistics of the  
519 selected companies. As the performance measures used for the companies  
520 were different from the performance measures used for the student data  
521 (with a direct real-life interpretation in the context of the given industry),  
522 expertly defined trapezoidal membership functions were used instead of the  
523 triangular membership functions used for the student data performance

524 assessment. The expert definitions also allowed for the appropriate  
525 reflection of the presence of an outlier (extremely low performance of one of  
526 the companies) in the net profit data. The trapezoidal membership  
527 functions (representing high, middle, and low performance) for the net  
528 profit values were defined by the expert as:  
529  $\mu_{low} \sim \Pi(x; -100, -100, -2, -0.5)$ ,  $\mu_{mid} \sim \Pi(x; -2, -0.5, 0.5, 2)$ , and  
530  $\mu_{high} \sim \Pi(x; 0.5, 2, 100, 100)$ . For  $DR_1$  and  $DR_2$ , the triangular membership  
531 function was created in a way analogous to the student data (i.e., using  $\alpha, \beta$   
532 and  $\gamma$ ).

533 To evaluate the validity of the hypotheses, we considered consistency  
534 values together with coverage values. In terms of consistency, high values  
535 were preferred, but the specific value of required consistency depended on  
536 the case we evaluated and on the consistency measure that was considered.  
537 Moreover, the evidence in favor of the hypotheses  $H_{01}, \dots, H_{09}$  was  
538 considered to be sufficient if the respective corresponding rules were  
539 significant and reasonable, in other words, if they have  $F_1$  consistency  
540 values ranged from acceptable (approximately 0.60 and higher), through  
541 high ( $\geq 0.75$ ), and to excellent ( $\geq 0.90$ ). In contrast, the rules with shallow  
542 consistency values were considered not indicative of the validity of the  
543 investigated hypothesis. In the evaluation, we gave priority to consistency  
544 first and then checked the coverage scores to gain additional support for the  
545 particular condition. Literally, the coverage was a set-theoretic parameter  
546 of practical importance (used to estimate how much cause covered the  
547 effect) (Ragin, 2008). With an acceptable  $F_1$  coverage, the reasonable cases  
548 ( $0.25 \leq \text{coverage} \leq 0.65$ ) were explained as high-performance. Even though

549 the priority was for the  $F_1$  set-theoretic scores in the evaluation and  
550 interpretation of the results of the analysis, we considered the reasonable  
551 values of the additional  $F_2$  measure provided a reliable confirmation of the  
552 given hypothesis. The  $F_4$  set-theoretic measures had a different  
553 interpretation than all the other measures; values over 0.5 were indicative of  
554 more evidence than counterevidence for the rule in the given data set. We  
555 interpreted the values of the calculated consistency and coverage measures  
556 in their mutual context. As such, this paper also shows the usefulness of  
557 the recently introduced  $F_4$  measures in practice.

558 All the calculations in the analysis were done using the Matlab 2018  
559 software. In order to do the calculations, we used built-in functions in the  
560 Matlab language (e.g., forming the triangular fuzzy sets), and the rest was  
561 programmed as local functions to perform the computations and store the  
562 results. The findings of this analysis with a discussion are presented in the  
563 next section.

### 564 **3. Results and discussion**

565 As we have driven our main analysis with the data from the student  
566 sample, we first discuss those results. The advantage of the student data  
567 was the environment in which it was obtained. A business simulation in a  
568 controlled classroom setting was repeatedly performed, and the effect of  
569 interfering variables could thus be minimized. Also, the artificial  
570 company-level and industry-level maps could be easily computed. The  
571 simulation context allowed for the assumption of full information  
572 concerning the industry-level cognition (the students and their groups as

573 stand-ins for companies were assumed to represent the full industry). A  
574 clear limitation of the use of student data is the questionable  
575 generalizability of the results. We have included students of  
576 business-oriented master’s programs, who can be assumed to be taking  
577 managerial positions in companies in the future, to provide a reasonable  
578 approximation to the real-life setting. Yet, their experience is limited in  
579 certain aspects. This, however, does not limit the possibility of analysing  
580 the usefulness of the proposed methodology as well as of the performance of  
581 the recently proposed measures ( $DR_2$ ,  $F_4$  consistency and coverage) on the  
582 data. We also present and discuss the results computed for the real-life  
583 company data in comparison to the findings from the analysis of the  
584 students’ data to show the relevance of the findings.

### 585 *3.1. Cognitive diversity among strategic decision makers within the company*

586 In this part, we investigate the possible links between within-company  
587 diversity and the performance of the company. The within-company  
588 diversity was operationalized as the average distance ratio ( $DR_1$  or  $DR_2$ ) of  
589 the cognitive maps of individual representatives of that company from the  
590 company-level cognitive map (the “average” of the individual cognitive  
591 maps represented by an adjacency matrix whose elements were the averages  
592 of the corresponding elements of the individual adjacency matrices).

#### 593 *3.1.1. Student sample*

594 The values of the set-theoretic scores calculated for the hypothesis  
595 analysis based on  $DR_1$  are summarized in Table B.2. It contains the overall  
596 consistency and coverage values calculated corresponding to each

597 conditional hypothesis.  $A \Rightarrow B$  denotes a conditional hypothesis established  
598 by the linguistics forms of  $DR_1$  and group performance. Hence, the first  
599 column represents the nine hypotheses developed initially and as an  
600 example, “High, High” means if  $DR_1$  was high, then the performance was  
601 expected to be high (the rest of them can be read in a similar way). In the  
602 table, “ $Cons_{F_i}$ ” refers to the consistency from each measure with the  $i$   
603 subscript of  $F$ ,  $i \in \{1, 2, 4\}$ , and similarly, “ $Cove_{F_i}$ ” refers to the coverage.

604 [Table 2 about here.]

605 In Table B.2, we can clearly see that only the rule of “High, High” had  
606 considerable support from the evidence, obtaining a  $Cons_{F_1}(H_{09})$  of 0.5934  
607 (that is close to the threshold) with a reasonable  $Cove_{F_1}(H_{09})$  of 0.3764. The  
608 rest of the consistency measures ( $Cons_{F_2} = 0.3580$  and  $Cons_{F_4} = 0.5118$ )  
609 also showed evidence in favor of  $H_{09}$ —namely,  $F_2$  suggests that there was non-  
610 ambivalent “pure evidence” in favor of this hypothesis, whereas  $Cons_{F_4} > 0.5$   
611 suggests that there was more evidence for “High $\Rightarrow$  High” than there is for  
612 “High  $\Rightarrow$  not-High.” Even though the evidence was not very strong, the  $H_{09}$   
613 rule and the corresponding hypothesis seemed to be supported by the student  
614 data the most when compared to the other hypotheses. There did not seem  
615 to be significant evidence of the support for the rest of the hypotheses (no  
616 other  $F_1$  consistency is close to the required 0.6 threshold, all the values of  
617 the  $F_4$  consistencies were below 0.5, indicating more evidence in favor of the  
618 negation of the rules instead of the rules themselves). Next, let us consider  
619 the findings based on the  $DR_2$  measure. Table B.3 illustrates the obtained  
620 results of the consistency and coverage values concerning the  $DR_2$  values for  
621 each hypothesis.

[Table 3 about here.]

The results in Table B.3 confirm what we observed from the  $DR_1$  results that high diversity raised performance. However, it is apparent that the  $DR_2$  results have produced slightly higher values of consistency and coverage than the  $DR_1$  regarding the hypothesis of  $H_{09}$ . We can also observe that while the  $Cons_{F_4}(H_{09})$  has increased with the use of  $DR_2$ , the values of  $Cons_{F_4}(H_{08})$  and  $Cons_{F_4}(H_{07})$  have decreased. From the construction of the  $F_4$  measures, this suggests that under  $DR_2$  the data support “High $\Rightarrow$  High” (i.e.,  $H_{09}$ ) more than any of the other hypotheses that could be summarized by “High $\Rightarrow$  not-High” (i.e.  $H_{08}$  or  $H_{07}$ ). Also this support was stronger than under the  $DR_1$  measure. By the same logic, we can conclude from the data in both tables that the case “High, Low” had the lowest consistencies, indicating that the high diversity did not seem to contribute to the low performance of the company. This was also evidenced by  $Cons_{F_4}(H_{07})$  being the closest to zero and well below 0.5. If we want to investigate what performance seemed to be the most supported by the data as a result of Middle within-company diversity, then the  $DR_1$ -based results suggest that  $H_{06}$  was the most consistent with the data ( $H_{06}$  had the highest  $F_1$  consistency of  $H_{06}$ ,  $H_{05}$ , and  $H_{04}$ ); however the  $F_4$  consistency of 0.4064 meant that “Middle $\Rightarrow$ not-High” had more support in the data than “Middle $\Rightarrow$ High.” This holds for the  $DR_2$ -based results as well, only the difference between the  $Cons_{F_1}(H_{06})$  and the values of  $Cons_{F_1}(H_{05})$  and  $Cons_{F_1}(H_{04})$  were even smaller, suggesting there was no evidence of a rule that would specify a particular performance level based on the within-firm diversity, as long as the diversity can be described as Middle. The results for the hypotheses mapping the possible outcome of

647 Low diversity were analogous; only the insignificantly more supported rule  
648 seemed to be  $H_{03}$ . Based on these results, there seemed to be weak support  
649 for the  $H_{09}$  hypothesis in the data.

650 To make this easier to understand, the results in Table B.2 and B.3 are  
651 visualized using bar graphs in Figure B.2 and B.3, respectively. From the  
652 figures, we can see the cases where there are high consistencies and reasonable  
653 coverages to be further investigated.

654 [Figure 2 about here.]

655 [Figure 3 about here.]

656 Highly diverse management teams in companies might have a broader  
657 range of attitudes, skills, and abilities, which could encourage addressing  
658 challenges and making correct and reasonable strategic decisions.  
659 Undoubtedly, the companies with such enthusiastic diverse teams could be  
660 enabled to be more innovative in the operation of a business that  
661 encounters an array of volatile, complex, ambiguous, unexpected situations.  
662 As a result, such companies might earn high performance in the market.  
663 Rationally, our finding supports the idea discussed in Reynolds and Lewis  
664 (2017). However, in the research of Roberson and Jeong (2007), they  
665 showed that there can be a curvilinear U-shaped relation between diversity  
666 and company performance as a whole. In our experimental data, we found  
667 that the high diversity in top management teams influenced a high  
668 improvement of the company performance. We did not see significant  
669 evidence that low diversity led to high performance or that a middle level of  
670 diversity supported the worst performance. The reason for the lack of

671 confirmation could be due to the partially artificial nature of the data.  
672 However, when we carefully inspect the results in Table B.2, we can see  
673 some evidence for the most consistent cause of low performance. Middle  
674 diversity might have had the highest consistencies causing low performance  
675 since we can see that  
676  $Cons_{F_1}(\text{Middle, Low}) > Cons_{F_1}(\text{Low, Low}) > Cons_{F_1}(\text{High, Low})$ . This  
677 appears in Table B.3 as well. This is something that supports (at least  
678 weakly) to the findings of Roberson and Jeong (2007).

### 679 3.1.2. Company sample

680 As we did above in our analysis on the student data, we performed the  
681 same analysis on the company data. The calculated values of the  
682 consistencies and coverages are presented in Table B.4 (based on  $DR_1$ ) and  
683 Table B.5 (based on  $DR_2$ ). From the results in the tables, it can be seen  
684 that the case “Low $\Rightarrow$ High” had the highest consistency,  
685  $Cons_{F_1}(H_{03}) = 0.7082$ , with a reasonable coverage,  $Cove_{F_1}(H_{03}) = 0.5537$ ,  
686 in comparison to the others. These scores clearly supported the existence of  
687 the relationship represented by  $H_{03}$ . Interestingly, as we can see in the  
688 results, the values of  $Cons_{F_1}$ ,  $Cons_{F_2}$  and  $Cons_{F_4}$  were identical. This is  
689 indicative of the expert definition of the fuzzy scale used for the description  
690 of company performance being such that it resulted in crisp memberships  
691 (0 and 1) of the performances of the companies in the given membership  
692 functions. Moreover, we had acceptable consistencies of 0.6066 and with a  
693 coverage of 1 reflecting a higher empirical support of the relationship “High  
694  $\Rightarrow$ Middle” from the  $DR_1$ -based results. This provided clear evidence to  
695 support the relationship “High  $\Rightarrow$ Middle” (this was also confirmed by the



696 results based on  $DR_2$ ). Also note, that even though “High  $\Rightarrow$ High” was not  
697 unambiguously supported by the data, the statement “High $\Rightarrow$ not-Low” has  
698 a consistency of 1 based on our data both under  $DR_1$  and  $DR_2$ . This  
699 suggests that the High within-company diversity ruled out the Low  
700 performance.

701 Even though we did not find consistency scores which reached the  
702 threshold of 0.6 from the rest of evidence, the consistency values on the  
703 relation “Middle $\Rightarrow$ Low” were again the highest from all that assumed  
704 Middle diversity as an antecedent of the rule. We can also clearly see that  
705 the support for “Middle $\Rightarrow$ Low” was higher than for its negation, in other  
706 words, “Middle $\Rightarrow$ not-Low” based on  $Cons_{F_4}(H_{04}) > 0.5$ . This suggests that  
707 there is at least some support for the validity of the hypothesis  $H_{04}$ .  
708 Furthermore, all consistencies and coverages on the relationships “High,  
709 Low”, “Middle, Middle” and “Low, Middle” were zero. This means we  
710 found no evidence from the results to support these relationships. Also, the  
711 findings with company data as student data supported the fact that  
712  $Cons_{F_1}(\text{Middle, Low}) > Cons_{F_1}(\text{Low, Low}) > Cons_{F_1}(\text{High, Low})$   
713 suggesting that the middle diversity had the strongest association with Low  
714 company performance based on the data. Generally, the evidence from the  
715 analysis of the company data seemed to support the findings of [Roberson](#)  
716 [and Jeong \(2007\)](#).

717 [Table 4 about here.]

718 [Table 5 about here.]

719 *3.2. Cognitive diversity between the companies within an industry*

720 *3.2.1. Student sample*

721 So far, we have discussed how the decision-makers within companies and  
722 the diversity of their cognitive frames affected the company performance  
723 across the results obtained over the analyses using the student and  
724 company data samples. We could have also abstracted from the individual  
725 level, considered companies to be the smallest analyzed units, and asked  
726 how the diversity within the industry (i.e., the differences of the strategic  
727 frames of the companies from the industry-level strategic frame) affected  
728 the performance of the companies. This was also possible with both our  
729 samples, as we could have easily used company-level cognitive maps (these  
730 were already available from the previous analysis) and their average as the  
731 industry-level cognitive map. The purpose of this analysis was to  
732 understand the impacts of the strategy frame of a company and its  
733 difference from the industry-level strategy frame on the performance of the  
734 company. We operationalized the company-industry cognitive diversity by  
735 the distance ratios ( $DR_1$  and  $DR_2$ ) of the company-level cognitive maps  
736 (an average cognitive map of all the students that represented the same  
737 company in the simulation task) from the industry-level one. We were  
738 again interested in the same set of possible relationships between such an  
739 understanding of cognitive diversity and company performance as  
740 summarized in Table B.1. Note that the difference from the previous  
741 analysis lies in the shift of the meaning of cognitive diversity; previously,  
742 the within-company diversity was considered, whereas we were now  
743 focusing on the diversity of companies within the given industry. Using the

744 distance ratios  $DR_1$  and  $DR_2$ , we have calculated the set-theoretic  $F_1, F_2,$   
745 and  $F_4$  consistency and coverage measures. The results which are based on  
746  $DR_1$  and  $DR_2$  are shown in Table B.6 and B.7, respectively.

747 [Table 6 about here.]

748 [Table 7 about here.]

749 According to the results (shown in Table B.6 and B.7), we can see that  
750 the student data did not offer many strong insights into the possible  
751 relationship of the difference of the strategic frames of the companies and  
752 the industry-level strategic frame with the performance of the companies.  
753 Under  $DR_1$ , the hypothesis most consistent with the data was  $H_{06}$ , based  
754 on its  $Cons_{F_1}(H_{06}) = 0.5722$  and the same held under  $DR_2$ , in this case,  
755  $Cons_{F_1}(H_{06}) = 0.6027$ . Even though this relationship seemed to pass the  
756 required consistency threshold for  $DR_2$ , the evidence in its favor could  
757 hardly be considered strong, as the support for “Middle $\Rightarrow$ High” was almost  
758 as strong in the data as the support for the negation of this relationship, in  
759 other words, for “Middle $\Rightarrow$ not-High”. A similar case was observed for  $H_{09}$   
760 in the previous analysis (where within-company diversity was considered).  
761 The performance of the company seemed to be rather unpredictable based  
762 on the cognitive diversity, as long as the diversity was high. As for the  
763 anticipated outcome of the Low cognitive diversity, the relationship  
764 “Low $\Rightarrow$ not-Low” seemed to have some support in the student data (note  
765 the rather low consistencies of  $H_{01}$ ). Apart from these findings, the results  
766 on the student data seemed to be rather inconclusive. The inconclusiveness  
767 of the results on student data might be due to the already mentioned low

768 experience of the student participants. This might have influenced the  
769 industry-level strategy frame represented by the collective cognitive map.  
770 In real-life data based on the much higher experience of the actual  
771 managers, the industry-level map might be different, and the cognitive  
772 diversity measured by the distance of the company's cognitive map from  
773 the industry-level one might then stress different aspects. While the  
774 interpretations of the results of the analysis and the example of the  
775 application of the proposed analytical methodology remain valid, we do not  
776 propose any practical implications of the student-based analysis in the  
777 context of within-industry diversity and its effect on company performance,  
778 due to the limits of the student sample and the limited ability to derive a  
779 meaningful industry-level cognitive frame from it. This should, however,  
780 not be an issue in real-life data obtained from companies, however we do  
781 have a representative sample of an industry at our disposal.

782

### 783 3.2.2. *Company sample*

784 We have investigated the same hypotheses concerning the effect of within-  
785 industry diversity and performance using the company data. The calculated  
786 values of the  $F_1$ ,  $F_2$ , and  $F_4$  set-theoretic consistency and coverage measures  
787 are shown in Table B.8 based on  $DR_1$  and Table B.9 based on  $DR_2$ .

788 [Table 8 about here.]

789 [Table 9 about here.]

790 As can be seen from Table B.8, both  $Cons_{F_1}(H_{03})$  and  $Cons_{F_1}(H_{09}) >$   
791 0.73 over the  $DR_1$ -based results. The results for  $H_{03}$  and  $H_{09}$  are even

792 stronger with the  $DR_2$ . Also, the  $DR_1$ -based  $Cove_{F_1}(H_{03}) = 0.3122$  and  
793  $Cove_{F_1}(H_{09}) = 0.5415$  provide reasonable empirical support in favor of each  
794 of these relationships. From the perspective of  $F_4$  measures, we can also see  
795 that the evidence in favor of the validity of  $H_{03}$  and  $H_{09}$  was much stronger  
796 than the evidence against these hypotheses. This can be interpreted as strong  
797 evidence which supported the existence of the relations “Low $\Rightarrow$ High” and  
798 “High $\Rightarrow$ High.”

799 Furthermore, we also had  $F_1$  consistency (0.6212 based on  $DR_1$  and  
800 0.6768 based on  $DR_2$ ) and coverage (0.6667 based on  $DR_1$  and 0.6768  
801 based on  $DR_2$ ) on the relation “Middle $\Rightarrow$ Low.” This suggests that the  
802 middle diversity between companies within an industry was associated with  
803 low performance of the company ( $H_{04}$ ). These findings are in agreement  
804 with what was weakly suggested by the student data in the within-company  
805 diversity context and what was clearly found in the company data in the  
806 same context. Overall, the presented results seem to be in line with  
807 [Roberson and Jeong \(2007\)](#), in other words, we have confirmed the  
808 possibility of existence of a curvilinear U-shaped relationship between  
809 cognitive diversity and company performance. This was now primarily  
810 supported by hypotheses  $H_{03}$ ,  $H_{09}$  (high performance in case of high  
811 diversity and low diversity), and also by  $H_{04}$  (which was indicating low  
812 performance for middle diversity). We thus extend the findings of [Roberson  
813 and Jeong \(2007\)](#), since our analysis was focused on differently defined  
814 cognitive diversity—mainly on the within-company and within-industry  
815 cognitive diversity.

#### 816 4. Conclusion

817 Theoretically, our findings contribute to the literature of strategic  
818 cognition by providing empirical evidence of the existence of a relationship  
819 between cognitive diversity and company performance. Regarding cognitive  
820 diversity among strategic decision-makers, our findings supported the  
821 findings of [Roberson and Jeong \(2007\)](#). It seems that more cognitive  
822 diversity within a decision-making team can lead to better levels of the  
823 performance. However high cognitive diversity might not be the only way  
824 towards high performance; low cognitive diversity seems to give strong  
825 grounds for high performance as well, and middle diversity can indicate  
826 lower performance. The reasons behind this can come from several possible  
827 sources (e.g., from competitive intensity and technological turbulence) and  
828 may moderate such relationships. Regarding cognitive diversity between  
829 companies in a market, we found support for the U-shaped relationship  
830 between cognitive diversity and company performance. This means that the  
831 companies with very different perceptions of the causalities leading to high  
832 performance compared to the dominant logic of the market are likely to  
833 perform well. They either find their market niche or are able to disrupt the  
834 market with their unique strategy. On the other hand, the companies that  
835 are cognitively at the core of the market's dominant logic also reach high  
836 levels of performance. The companies with a middle level of distance from  
837 the market's dominant logic are the most likely to perform poorly. We also  
838 found this with the company data as our  $H_{04}$  hypothesis ("Middle  $\Rightarrow$   
839 Low") was supported.

840 Methodologically, we contribute to the study of managerial cognition by

841 demonstrating how relationships regarding managerial cognitive diversity  
842 (within and between companies) can be empirically assessed even with  
843 small sample sizes. The proposed method enables the examination of the  
844 relationship between managerial-level cognition and company performance  
845 and then suggests what could be understood of the impact of diversity to  
846 achieve better performance during operations in the market. This approach  
847 supports managers and organizations in gaining insight into management  
848 team operations and how they affect performance within market change.  
849 Notably, this proposed method has the potential to study how diversity  
850 through individuals' thoughts, abilities, and skills are meaningful to  
851 changes in the industry. The method is based on using fuzzy set-theory,  
852 concepts in fsQCA, and distance ratio measures, thus, it can be an efficient  
853 tool for producing precise measures to make decisions at first sight.

854 While introducing a novel methodology, this research aimed to explore the  
855 relation between managerial-level cognition and industry-level performance  
856 through shared cognitive maps produced by students in a strategic decision-  
857 making process in a controlled setting of a business simulation. In addition  
858 to that, we introduced nine hypotheses based on the diversity (high-middle-  
859 low) and performance (high-middle-low) to be tested under two different  
860 definitions of cognitive diversity, within-company and within-industry. To  
861 do so, a total of 431 cognitive maps were created for this study. The maps  
862 were produced by the teams of graduate students in outlining their beliefs,  
863 views, and decisions in a strategic issues operation. In the analytical phase,  
864 we deployed two distance ratio measures and innovative techniques in fsQCA.

865 In the analysis, we first investigated how the cognitive diversity between

866 strategic decision-makers within a company affected company performance.  
867 From the empirical evidence obtained, the first results with the student  
868 sample suggested that there might be an impact of high-level cognitive  
869 diversity on the enhancement of the performance of the company in a  
870 market. We also tested our method with real company data in which the  
871 cognitive maps were produced by managers in nine selected companies in  
872 Finland. From the results in the analysis of these shared cognitive maps, it  
873 was confirmed with sufficient evidence that low cognitive diversities of the  
874 experts led to high company performance. The findings from both results  
875 corroborated what was revealed by [Roberson and Jeong \(2007\)](#). Next, we  
876 did an analysis to study the relation of the diversity between companies  
877 within an industry to company performance. In this investigation, even  
878 though the results for the student data were inconclusive, possibly due to  
879 the limitations of the sample, we managed to find conclusive results for the  
880 real-life company data. We managed to found evidence in favor of the  
881 curvilinear U-shaped relation ([Roberson and Jeong, 2007](#)) of the diversity  
882 between companies within an industry with company performance.

883 Despite its exploratory nature, this study has offered some insight into  
884 our understanding of the novel distance ratio measure ( $DR_2$ ) by [Bergman](#)  
885 [et al. \(2020\)](#) and set-theoretic scores ( $F_2$  and  $F_4$ ) by [Stoklasa et al. \(2017,](#)  
886 [2018\)](#). As far as we know, this is the first time that the distance ratios  
887 together with the fsQCA have been used to explore the knowledge from the  
888 strategic cognitive frames. In doing so, we demonstrated that the distance  
889 ratio measures with the fsQCA approaches are powerful techniques for  
890 analysing cognitive maps and cognitive diversity in the maps.



891 A number of possible future studies using the proposed approach are  
892 apparent. For example, it would be interesting to assess the effects of  
893 cognition and the decisions of persons who are at the top level in the  
894 organization as they dominate an organization's cognitive operations. In  
895 addition, market influences, institutional affiliations of directors, tourism  
896 policies, processes in manufacturing systems, and so on can be  
897 conceptualized in cognitive frames and then could drive examinations to  
898 produce useful information. All in all, we are confident that the method  
899 introduced can be used for future studies on the current topics related to  
900 cognitive mapping and the evaluation of cognitive maps in a wide range of  
901 real-world applications.

## 902 **Appendix A.**

903 [Table 10 about here.]

## 904 **Appendix B.**

905 [Table 11 about here.]

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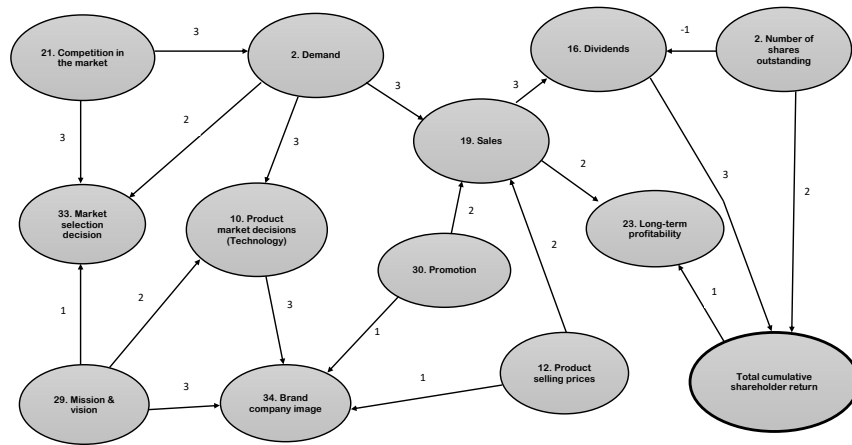


Figure B.1: An example of a cognitive map in the original data of the study, as provided by the students in the business simulation task.

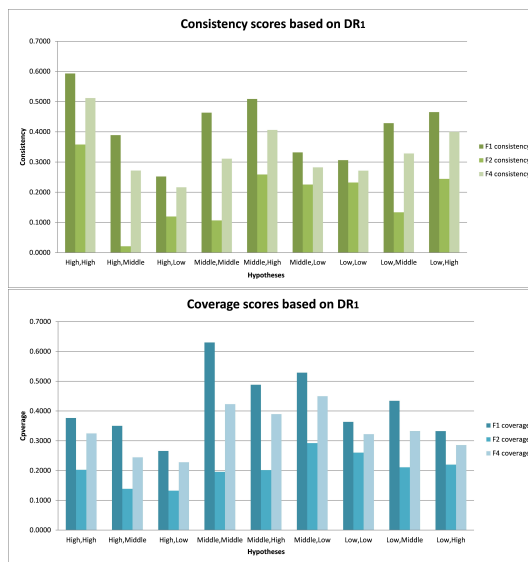


Figure B.2: Results of consistency and coverage values based on  $DR_1$  in the evaluation of the hypotheses.

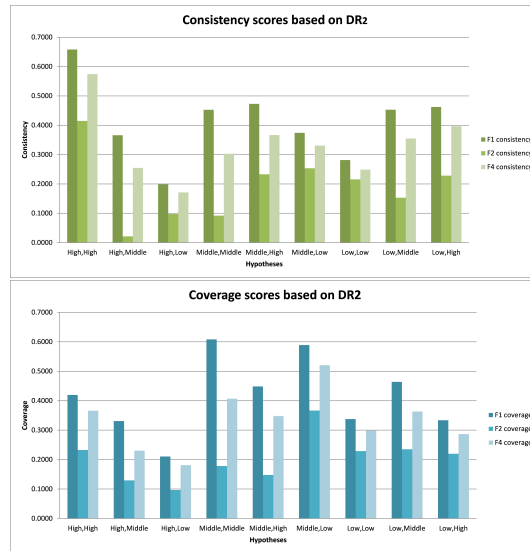


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Table B.1: The hypothesis models in linguistic levels with distance ratios and group performance.

		<i>Group Performance</i>		
		low	middle	high
<i>DR</i>	low	$H_{01}$	$H_{02}$	$H_{03}$
	middle	$H_{04}$	$H_{05}$	$H_{06}$
	high	$H_{07}$	$H_{08}$	$H_{09}$

Table B.2: The results of the consistencies and coverages obtained over the  $DR_1$  for all the hypotheses with the student data, when the within-company diversity was considered.

$DR_1$ based consistency and coverage values							
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$	
$(H_{09})$ <b>High, High</b>	<b>0.5934</b>	<b>0.3764</b>	<b>0.3580</b>	<b>0.2026</b>	<b>0.5118</b>	<b>0.3247</b>	
$(H_{08})$ High, Middle	0.3891	0.3499	0.0211	0.1387	0.2716	0.2443	
$(H_{07})$ High, Low	0.2522	0.2659	0.1197	0.1325	0.2164	0.2281	
$(H_{05})$ Middle, Middle	0.4635	0.6300	0.1065	0.1956	0.3112	0.4229	
$(H_{06})$ Middle, High	0.5091	0.4879	0.2587	0.2016	0.4064	0.3895	
$(H_{04})$ Middle, Low	0.3320	0.5288	0.2254	0.2921	0.2823	0.4496	
$(H_{01})$ Low, Low	0.3063	0.3635	0.2321	0.2602	0.2714	0.3221	
$(H_{02})$ Low, Middle	0.4286	0.4341	0.1335	0.2109	0.3285	0.3326	
$(H_{03})$ Low, High	0.4653	0.3323	0.2443	0.2198	0.3999	0.2856	



Table B.3: The results of the consistencies and coverages obtained over the  $DR_2$  for all the hypotheses with the student data, when the within-company diversity was considered.

$DR_2$ based consistency and coverage values							
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$	
$(H_{09})$ <b>High, High</b>	<b>0.6582</b>	<b>0.4195</b>	<b>0.4147</b>	<b>0.2326</b>	<b>0.5744</b>	<b>0.3661</b>	
$(H_{08})$ High, Middle	0.3660	0.3308	0.0211	0.1293	0.2546	0.2300	
$(H_{07})$ High, Low	0.1987	0.2104	0.0972	0.0967	0.1710	0.1811	
$(H_{05})$ Middle, Middle	0.4526	0.6082	0.0919	0.1782	0.3028	0.4068	
$(H_{06})$ Middle, High	0.4730	0.4483	0.2328	0.1476	0.3667	0.3475	
$(H_{04})$ Middle, Low	0.3741	0.5890	0.2536	0.3666	0.3305	0.5205	
$(H_{01})$ Low, Low	0.2814	0.3377	0.2155	0.2289	0.2487	0.2984	
$(H_{02})$ Low, Middle	0.4530	0.4638	0.1529	0.2352	0.3547	0.3631	
$(H_{03})$ Low, High	0.4622	0.3338	0.2281	0.2200	0.3966	0.2864	

Table B.4: The results of the consistencies and coverages obtained over the  $DR_1$  for all the hypotheses for the company data.

$DR_1$ based consistency and coverage values						
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$
$(H_{09})$ High, High	0.3934	0.1297	0.3934	0.0000	0.3934	0.1297
$(H_{08})$ <b>High, Middle</b>	<b>0.6066</b>	<b>1.0000</b>	<b>0.6066</b>	<b>1.0000</b>	<b>0.6066</b>	<b>1.0000</b>
$(H_{07})$ High, Low	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{05})$ Middle, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{06})$ Middle, High	0.4599	0.3166	0.4599	0.1406	0.4599	0.3166
$(H_{04})$ Middle, Low	0.5401	0.6198	0.5401	0.2808	0.5401	0.6198
$(H_{01})$ Low, Low	0.2918	0.3802	0.2918	0.0411	0.2918	0.3802
$(H_{02})$ Low, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{03})$ <b>Low, High</b>	<b>0.7082</b>	<b>0.5537</b>	<b>0.7082</b>	<b>0.5073</b>	<b>0.7082</b>	<b>0.5537</b>

Table B.5: The results of the consistencies and coverages obtained over the  $DR_2$  for all the hypotheses for the company data.

$DR_2$ based consistency and coverage values						
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$
$(H_{09})$ High, High	0.4439	0.1597	0.4439	0.0000	0.4439	0.1597
$(H_{08})$ High, Middle	0.5561	1.0000	0.5561	1.0000	0.5561	1.0000
$(H_{07})$ High, Low	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{05})$ Middle, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{06})$ Middle, High	0.4372	0.2887	0.4372	0.0807	0.4372	0.2887
$(H_{04})$ Middle, Low	0.5628	0.6195	0.5628	0.3334	0.5628	0.6195
$(H_{01})$ Low, Low	0.2928	0.3805	0.2928	0.0945	0.2928	0.3805
$(H_{02})$ Low, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{03})$ <b>Low, High</b>	<b>0.7072</b>	<b>0.5516</b>	<b>0.7072</b>	<b>0.5032</b>	<b>0.7072</b>	<b>0.5516</b>

Table B.6: The results of the consistencies and coverages obtained over the  $DR_1$  for all the hypotheses for the student data, with diversity operationalized by the distance ratio of the company-level cognitive map and the industry-level one.

$DR_1$ based consistency and coverage values						
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$
$(H_{09})$ High, High	0.4056	0.2963	0.2292	0.1790	0.3631	0.2653
$(H_{08})$ High, Middle	0.3620	0.3749	0.0817	0.1952	0.2859	0.2961
$(H_{07})$ High, Low	0.3846	0.4668	0.2807	0.2417	0.3510	0.4260
$(H_{05})$ Middle, Middle	0.3692	0.5378	0.0882	0.2341	0.2777	0.4045
$(H_{06})$ Middle, High	0.5722	0.5879	0.3674	0.3716	0.5107	0.5247
$(H_{04})$ Middle, Low	0.2416	0.4124	0.1654	0.1392	0.2116	0.3613
$(H_{01})$ Low, Low	0.2444	0.2230	0.1509	0.1749	0.2331	0.2127
$(H_{02})$ Low, Middle	0.4544	0.3539	0.1105	0.2299	0.3845	0.2994
$(H_{03})$ Low, High	0.4411	0.2423	0.1907	0.1432	0.3825	0.2101

Table B.7: The results of the consistencies and coverages obtained over the  $DR_2$  for all the hypotheses for the student data, with diversity operationalized by the distance ratio of the company-level cognitive map and the industry-level one.

$DR_2$ based consistency and coverage values						
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$
$(H_{09})$ High, High	0.3999	0.3211	0.2006	0.1642	0.3450	0.2771
$(H_{08})$ High, Middle	0.3961	0.4511	0.0912	0.2317	0.3095	0.3524
$(H_{07})$ High, Low	0.3774	0.5036	0.2716	0.2872	0.3455	0.4611
$(H_{05})$ Middle, Middle	0.3526	0.4824	0.0775	0.1787	0.2496	0.3416
$(H_{06})$ <b>Middle, High</b>	<b>0.6027</b>	<b>0.5816</b>	<b>0.4014</b>	<b>0.3422</b>	<b>0.5323</b>	<b>0.5137</b>
$(H_{04})$ Middle, Low	0.2506	0.4018	0.1768	0.1090	0.2180	0.3496
$(H_{01})$ Low, Low	0.2222	0.1990	0.1283	0.1226	0.2114	0.1893
$(H_{02})$ Low, Middle	0.4556	0.3482	0.1168	0.2639	0.4005	0.3060
$(H_{03})$ Low, High	0.4325	0.2331	0.1876	0.1507	0.3882	0.2092

Table B.8: The results of the consistencies and coverages obtained over the  $DR_1$  for all the hypotheses for the company data, with diversity operationalized by the distance ratio of the company-level cognitive map and the industry-level one.

$DR_2$ based consistency and coverage values						
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$
$(H_{09})$ <b>High, High</b>	<b>0.7303</b>	<b>0.5415</b>	<b>0.7303</b>	<b>0.4829</b>	<b>0.7303</b>	<b>0.5415</b>
$(H_{08})$ High, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{07})$ High, Low	0.2697	0.3333	0.2697	0.1707	0.2697	0.3333
$(H_{05})$ Middle, Middle	0.1515	0.4878	0.1515	0.0000	0.1515	0.4878
$(H_{06})$ Middle, High	0.2273	0.1463	0.2273	0.0000	0.2273	0.1463
$(H_{04})$ <b>Middle, Low</b>	<b>0.6212</b>	<b>0.6667</b>	<b>0.6212</b>	<b>0.5041</b>	<b>0.6212</b>	<b>0.6667</b>
$(H_{01})$ Low, Low	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
$(H_{02})$ Low, Middle	0.2471	0.5122	0.2471	0.0244	0.2471	0.5122
$(H_{03})$ <b>Low, High</b>	<b>0.7529</b>	<b>0.3122</b>	<b>0.7529</b>	<b>0.2244</b>	<b>0.7529</b>	<b>0.3122</b>

Table B.9: The results of the consistencies and coverages obtained over the  $DR_2$  for all the hypotheses for the company data, with diversity operationalized by the distance ratio of the company-level cognitive map and the industry-level one.

$DR_2$ based consistency and coverage values							
$A \Rightarrow B$	$Cons_{F_1}$	$Cove_{F_1}$	$Cons_{F_2}$	$Cove_{F_2}$	$Cons_{F_4}$	$Cove_{F_4}$	
$(H_{09})$ <b>High, High</b>	<b>0.7460</b>	<b>0.5697</b>	<b>0.7460</b>	<b>0.5394</b>	<b>0.7460</b>	<b>0.5697</b>	
$(H_{08})$ High, Middle	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	
$(H_{07})$ High, Low	0.2540	0.3232	0.2540	0.1919	0.2540	0.3232	
$(H_{05})$ Middle, Middle	0.1616	0.4848	0.1616	0.0000	0.1616	0.4848	
$(H_{06})$ Middle, High	0.1616	0.0970	0.1616	0.0000	0.1616	0.0970	
$(H_{04})$ <b>Middle, Low</b>	<b>0.6768</b>	<b>0.6768</b>	<b>0.6768</b>	<b>0.5455</b>	<b>0.6768</b>	<b>0.6768</b>	
$(H_{01})$ Low, Low	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	
$(H_{02})$ Low, Middle	0.2361	0.5152	0.2361	0.0303	0.2361	0.5152	
$(H_{03})$ <b>Low, High</b>	<b>0.7639</b>	<b>0.3333</b>	<b>0.7639</b>	<b>0.2667</b>	<b>0.7639</b>	<b>0.3333</b>	

Table B.10: Pool of strategic topics on sustainable return to shareholders.

ID	Company's strategic issues	ID	Company's strategic issues
1	Market share	21	Competition in the market
2	Demand	22	Short-term profitability
3	Own manufacturing	23	Long-term profitability
4	Contract manufacturing	24	Growth of the company
5	Inventory management	25	Employee training and education
6	Investment in production and plants	26	Consumer price elasticity
7	Number of R&D personnel	27	R&D employee turnover
8	In-house R&D	28	Wages of R&D employees
9	Buying technology and design licenses	29	Mission and vision
10	Product-market decisions (technology)	30	Promotion
11	Feature offered	31	Transportation cost
12	Product selling prices	32	Interest rates
13	Logistics priorities	33	Market selection decisions
14	Transfer prices	34	Brand, company image
15	Long-term debt	35	Capacity allocation
16	Dividends	36	Network coverage
17	Number of shares outstanding	37	Equity ratio
18	Interest loans	38	Environmental sustainability
19	Sales	39	Supplier selection
20	Corporate tax rate	40	Supply chain ethics



Table B.11: An example of a  $41 \times 41$  adjacency matrix.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	...	36	37	38	39	40	41
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	3
2	0	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0	0	...	0	0	0	0	0	2
3	0	0	0	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0	...	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
8	0	0	2	0	0	0	0	0	0	0	3	0	0	0	0	0	0	0	...	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	1
11	0	0	0	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0	...	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
15	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	...	0	-2	0	0	0	-1
16	0	0	0	0	0	0	0	-2	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	3
17	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	-1	0	0	...	0	0	0	0	0	1
18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
.	.	.	.	.	.	.	.	.	.	.	.	.	.	.	.	.	.	.	...	.	.	.	.	.	.
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36	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
37	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
38	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0
39	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	1	0
40	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	-1	0	0	0
41	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	...	0	0	0	0	0	0